

Tennessee Operator Certification Formula Manual

Water Treatment Formulas & Conversions

 $Prepared \ by \ the \ Fleming \ Training \ Center$

About This Manual

This publication is provided by the Tennessee Department of Environment and Conservation (TDEC), Division of Water Resources (DWR), as an official resource for examinees participating in the State of Tennessee's operator certification program. It may be used during certification exams and is intended to support operators in understanding and applying essential mathematical formulas and conversions in the field.

This manual was collaboratively developed and reviewed by:

- Fleming Training Center (FTC) content development and formatting
- Water Professionals International (WPI) foundational formula reference materials
- Tennessee Association of Utility Districts (TAUD) editorial review and industry input

This resource is intended to reflect Tennessee's commitment to operator preparedness and professional excellence. While based on national standards, the formatting and presentation have been tailored to meet the needs of Tennessee operators and exam settings.

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Circumference and Perimeter

Circumference of a Circle = (3.14)(Diameter)

Perimeter, ft = (2)(Length, ft) + (2)(Width, ft)

Area

Area of a Circle*, $ft^2 = (0.785)(Diameter, ft)^2$

Area of a Circle, $ft^2 = (3.14)(Radius, ft)^2$

Area of a Rectangle*, ft² =(Length, ft)(Width, ft)

Area of a Right Triangle*, $ft^2 = \frac{[(Base, ft)(Height, ft)]}{2}$

Lateral Surface Area of a Cone, $ft^2 = (3.14)(Radius, ft)(\sqrt{(Radius, ft)^2 + (Height, ft)^2})$

Total Surface Area of a Cone, $ft^2 = (3.14)(Radius, ft) \left(Radius, ft + \sqrt{(Radius, ft)^2 + (Height, ft)^2}\right)$

Total Exterior Surface Area of a Cylinder, ft² =

(end #1 SA, ft²)+(end #2 SA, ft²)+[(3.14)(Diameter, ft)(Height, ft)]

Where SA = Surface Area of a Circle

<u>Volume</u>

Volume of a Cone, $ft^3 = (1/3)(0.785)$ (Diameter, $ft)^2$ (Height, ft)

Volume of a Cylinder, $ft^3 = (0.785)(Diameter, ft)^2(Height, ft)$

Volume of a Rectangular Tank, ft³ = (Length, ft)(Width, ft)(Height, ft)

Volume, gallons = $(Volume, ft^3)(7.48 \text{ gal/ft}^3)$

<u>Velocity</u>

Velocity, ft/sec =
$$\frac{\text{Distance, ft}}{\text{Time, sec}}$$

Velocity, ft/sec =
$$\frac{\text{Flow Rate, ft}^3/\text{sec}}{\text{Area, ft}^2}$$

^{*}Pie Wheel Format for this equation is available at the end of this document

Flow

Flow*, $ft^3/sec = (Area, ft^2) (Velocity, ft/sec)$

Flow Through a Channel, ft³/sec = (Width, ft)(Depth, ft)(Velocity, ft/sec)

Flow Through a Full Pipeline, $ft^3/sec = (0.785)(Diameter, ft)^2(Velocity, ft/sec)$

Flow Through a Cone, $ft^3/sec = (1/3)(0.785)(Diameter, ft)^2(Velocity, ft/sec)$

Pounds

Mass*, lb = (Concentration, mg/L)(Volume, MG)(8.34 lb/gal)

Mass, lb =
$$\frac{\text{(Concentration, mg/L)(Volume, MG)(8.34 lb/gal)}}{\text{Chemical Purity, % expressed as a decimal}}$$

Loading Rate*, lb/day = (Concentration, mg/L)(Flow, MGD)(8.34 lb/gal)

Feed Rate,
$$lb/day = \frac{(Dosage, mg/L)(Flow, MGD)(8.34 lb/gal)}{Chemical Purity, % expressed as a decimal}$$

Fluoride Feed Rate, lb/day =

(Dosage, mg/L)(Flow, MGD)(8.34 lb/gal)

(Available Fluoride Ion, % expressed as a decimal)(Purity, % expressed as a decimal)

Fluoride Saturator Feed Rate, gpm =
$$\frac{\text{(Plant Capacity, gpm)(Dosage, mg/L)}}{18,000 \text{ mg/L}}$$

Dosage

Dosage, mg/L =
$$\frac{\text{(Feed Rate, lb/day)}}{\text{(Flow, MGD)(8.34 lb/gal)}}$$

Dosage, mg/L =
$$\frac{\text{(Feed Rate, lb/day)(Chemical Purity, \% expressed as decimal)}}{\text{(Flow, MGD)(8.34 lb/gal)}}$$

Dosage,
$$mg/L = \frac{\text{(Feed Rate, Ib)(Chemical Purity, % expressed as decimal)}}{\text{(Volume, MG)(8.34 lb/gal)}}$$

Fluoride Dosage, mg/L =

(Feed Rate, lb/day)(Available Fluoride Ion, % expressed as a decimal)(Purity, % expressed as a decimal)

(Flow, MGD)(8.34 lb/gal)

Fluoride Saturator Dosage, mg/L =
$$\frac{\text{(Feed Rate, gpm)(18,000 mg/L)}}{\text{Flow, gpm}}$$

^{*}Pie Wheel Format for this equation is available at the end of this document

Power

$$Amps = \frac{Volts}{Ohms}$$

Amps (Single-Phase) =
$$\frac{(746 \text{ watts/HP})(\text{Horsepower})}{(\text{Volts})(\text{Efficiency}, \% \text{ as a decimal})(\text{Power Factor})}$$

Amps (Three-Phase) =
$$\frac{(746 \text{ watts/HP})(\text{Horsepower})}{(1.732)(\text{Volts})(\text{Efficiency}, \% \text{ as a decimal})(\text{Power Factor})}$$

Cost, \$/hour = (Motor Horsepower, hp)(0.746 kW/hp)(Cost, \$/kW-hr)

Electromotive Force*, volts = (Current, amps)(Resistance, ohms)

Horsepower =
$$\frac{\text{(Volts)(Amps)}}{\text{(746 watts/HP)}}$$

Power, watts (AC Circuit) = (Volts)(Amps)(Power Factor)

Power, watts (DC Circuit)= (Volts)(Amps)

Power Factor =
$$\frac{\text{Watts}}{\text{(Volts)(Amps)}}$$

Pumps and Motors

Pumping Rate

Pumping Rate, gal/min =
$$\frac{\text{Volume, gal}}{\text{Time, min}}$$

Pumping Rate of a Rectangular Tank, gal/min =
$$\frac{\text{(Length, ft)(Width, ft)(Depth, ft)} \left(7.48 \text{ gal/ft}^3\right)}{\text{Time, min}}$$

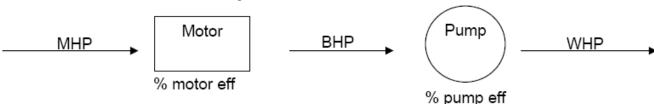
Pumping Rate of a Cylindrical Tank, gal/min =
$$\frac{(0.785)(\text{Diameter, ft})^2(\text{Depth, ft})\left(7.48 \text{ gal/ft}^3\right)}{\text{Time, min}}$$

Pumping Rate of a Conical Tank, gal/min =
$$\frac{(1/3)(0.785)(\text{Diameter, ft})^{2}(\text{Depth, ft})(7.48 \text{ gal/ft}^{3})}{\text{Time, min}}$$

Time to Fill, min =
$$\frac{\text{Tank Volume, gal}}{\text{Flow Rate, gal/min}}$$

^{*}Pie Wheel Format for this equation is available at the end of this document

Pumps and Motors (continued)



Horsepower

Water Horsepower, hp =
$$\frac{\text{(Flow, gpm)(Head, ft)}}{(3,960)}$$

Brake Horsepower, hp =
$$\frac{\text{(Flow, gpm)(Head, ft)}}{\text{(3,960)(Pump Efficiency, % expressed as a decimal)}}$$

Brake Horsepower, hp =
$$\frac{\text{Water Horsepower, hp}}{\text{Pump Efficiency, } \% \text{ expressed as a decimal}}$$

Motor Horsepower, hp =
$$\frac{\text{(Flow, gpm)(Head, ft)}}{\text{(3,960)(Pump Efficiency, % as a decimal)(Motor Efficiency, % as a decimal)}}$$

Motor Horsepower, hp =
$$\frac{\text{Water Horsepower, hp}}{\text{(Pump Efficiency, % as a decimal)}(\text{Motor Efficiency, % as a decimal)}}$$

Motor Horsepower,
$$hp = \frac{Brake \text{ Horsepower, } hp}{Motor \text{ Efficiency, } \% \text{ expressed as a decimal}}$$

Efficiency

Efficiency,
$$\% = \frac{\text{Horsepower Output, hp}}{\text{Horsepower Supplied, hp}} \times 100\%$$

Motor Efficiency,
$$\% = \frac{\text{Brake Horsepower, hp}}{\text{Motor Horsepower, hp}} \times 100\%$$

Pump Efficiency,
$$\% = \frac{\text{Water Horsepower, hp}}{\text{Brake Horsepower, hp}} \times 100\%$$

Wire-to-Water Efficiency, % =

(Pump Efficiency, % as a decimal)(Motor Efficiency, % as a decimal)(100%)

Wire-to-Water Efficiency,
$$\% = \frac{\text{Water Horsepower, hp}}{\text{Motor Horsepower, hp}} \times 100\%$$

Wire-to-Water Efficiency,
$$\% = \frac{\text{(Flow, gpm)(Total Dynamic Head, ft)}(0.746 \text{ kW/hp})}{(3,960)(\text{Electrical Demand, kW})} \times 100\%$$

Chlorination

CT Calculation = (Disinfectant Residual Concentration, mg/L)(Time,min)

Chlorine Dose, mg/L = Chlorine Demand, mg/L + Chlorine Residual, mg/L

Dosage, mg/L =
$$\frac{\text{(Feed Rate, lb/day)(Chemical Purity, \% expressed as a decimal)}}{\text{(Flow, MGD)(8.34 lb/gal)}}$$

Feed Rate,
$$lb/day = \frac{(Dosage, mg/L)(Flow, MGD)(8.34 lb/gal)}{Chemical Purity, % expressed as a decimal}$$

$$Hypochlorite \ Feed \ Rate, \ gpd = \frac{(Dosage, \ mg/L)(Flow, \ MGD)(8.34 \ lb/gal)}{(Chemical \ Purity,\% \ expressed \ as \ a \ decimal)(Solution \ Density, \ lb/gal)}$$

Hypochlorite Strength,
$$\% = \frac{\text{Chlorine Required, lb}}{\text{(Hypochlorite Solution Needed, gal)(8.34 lb/gal)}} \times 100\%$$

Substitution of Bleach for Chlorine Gas, gal =

Chlorine Feed, lb

(Available Chlorine from Bleach, % expressed as a decimal)(8.34 lb/gal)

Substitution of Bleach for HTH, gal =

(Available Chlorine from HTH, % expressed as a decimal)(HTH Feed, lb) (Available Chlorine from Bleach, % expressed as a decimal)(8.34 lb/gal)

Substitution of HTH for Bleach, lb =

(Available Chlorine from Bleach, % expressed as a decimal)(Bleach, gal)(8.34 lb/gal)

Available Chlorine from HTH, % expressed as a decimal

Substitution of HTH for Chlorine gas,
$$lb = \frac{Chlorine Feed, lb}{Available Chlorine from HTH, % expessed as a decimal}$$

Well Formulas

Well Yield, gal/min =
$$\frac{\text{Volume, gal}}{\text{Time, min}}$$

Drawdown, ft = Pumping Water Level, ft – Static Water Level, ft

Specific Capacity, gpm/ft =
$$\frac{\text{Well Yield, gal/min}}{\text{Drawdown, ft}}$$

Coagulation/Flocculation

Detention Time =
$$\frac{\text{(Volume)}}{\text{Flow}}$$

Detention Time,
$$sec = \frac{(Volume, gal)(1440 min/day)(60 sec/min)}{Flow, gpd}$$

Detention Time, min =
$$\frac{\text{(Volume, gal)}(1440 \text{ min/day)}}{\text{Flow, gpd}}$$

Dosage, mg/L =
$$\frac{\text{(Feed Rate, lb/day)(Chemical Purity, } \% \text{ expressed as decimal)}}{\text{(Flow, MGD)(8.34 lb/gal)}}$$

Feed Rate,
$$lb/day = \frac{(Dosage, mg/L)(Flow, MGD)(8.34 lb/gal)}{Chemical Purity, % expressed as a decimal}$$

Sedimentation

Detention Time =
$$\frac{\text{(Volume)}}{\text{Flow}}$$

Detention Time,
$$hr = \frac{\text{(Volume, gal)}(24 \text{ hr/day)}}{\text{Flow, gpd}}$$

Hydraulic Loading Rate, gpd/ft² =
$$\frac{\text{Total Flow Applied, gpd}}{\text{Area. ft}^2}$$

Surface Loading (Overload) Rate,
$$gpd/ft^2 = \frac{Flow, gpd}{Surface Area, ft^2}$$

Weir Overflow Rate

Weir Overflow Rate,
$$gpd/ft = \frac{Flow, gpd}{Weir Length, ft}$$

Length of Circular Weir, ft = (3.14)(Diameter, ft)

Solids Removal

Reduction in Flow,
$$\% = \frac{\text{(Original Flow - Reduced Flow)}}{\text{Original Flow}} \times 100\%$$

Removal,
$$\% = \frac{\text{(In-Out)}}{\text{In}} \times 100\%$$

Solids, mg/L =
$$\frac{\text{(Dry Solids, g)(1,000,000)}}{\text{Sample Volume, mL}}$$

Solids Concentration, mg/L =
$$\frac{\text{Weight, mg}}{\text{Volume, L}}$$

Filtuatio

Filtration

Filter Yield, $lb/hr/ft^2 = \frac{(Solids\ Loading,\ lb/day)(Recovery,\ \%\ expressed\ as\ decimal)}{(Filter\ Operation,\ hr/day)(Area,\ ft^2)}$

Filter Drop Test Velocity, ft/min = $\frac{\text{Water Drop, ft}}{\text{Time of Drop, min}}$

Backwashing

Backwash Water Volume, gal = (Backwash Rate, gpm/ft²)(Backwash Time, min)(Filter Area, ft²)

Backwash Water,
$$\% = \frac{\text{Backwash Water, gal}}{\text{Water Filtered, gal}} \times 100\%$$

Filter Backwash Rise Rate, in/min =
$$\frac{\left(\text{Backwash Rate, gpm/ft}^2\right)(12 \text{ in/ft})}{7.48 \text{ gal/ft}^3}$$

Hook Gauge

Volume, gal = (Filter Length, ft)(Filter Width, ft)(Water Drop or Rise, ft)(7.48 gal/ft³)

Filtration Rate, gal/min =
$$\frac{\text{Volume, gal}}{\text{Average Time, min}}$$

Filter Bed Area, ft² = (Filter Bed Length, ft)(Filter Bed Width, ft)

Filter Loading Rate,
$$gpm/ft^2 = \frac{Flow, gpm}{Filter Area, ft^2}$$

Solution Preparation

Concentration =
$$\frac{\text{Concentration, lb/gal}}{\text{Density, lb/gal}} \times 100\%$$

Percent Strength, % (by weight) =
$$\frac{\text{Weight of Chemical, lbs}}{\text{(Weight of Water, lbs + Weight of Chemicals, lbs)}} \times 100\%$$

Three Normal or Blending
$$(C_1 \times V_1) + (C_2 \times V_2) = (C_3 \times V_3)$$

Where C = Concentration or Normality

Two Normal Equation (Dilution)
$$(C_1 \times V_1) = (C_2 \times V_2)$$

Units must be compatible

and V = Volume

Chemicals, lbs =
$$\frac{\text{(Water Volume, gal} \times 8.34lb/gal)\text{(Desired Concentration, %)}}{\text{(100%-Desired Concentration, %)}}$$

Water Volume, gal =
$$\frac{\text{(Chemical, lbs)(100\%-Desired Concentration, \%)}}{\text{(Desired Concentration, \%)(8.34 lb/gal)}}$$

Chemical Feeders

Chemical Feed Pump Setting, % stroke = $\frac{\text{Desired flow}}{\text{Maximum flow}} \times 100\%$

Chemical Feed Pump Setting, mL/min =

(Flow, MGD)(Dose, mg/L)(3.785 L/gal)(1,000,000 gal/MG)

(Chemical Density, mg/mL)(Active Chemical, % expressed as a decimal)(1440 min/day)

Dosage, mg/L =
$$\frac{\text{(Feed Rate, lb/day)(Chemical Purity, \% expressed as decimal)}}{\text{(Flow, MGD)(8.34 lb/gal)}}$$

Feed Rate,
$$lb/day = \frac{(Dosage, mg/L)(Flow, MGD)(8.34 lb/gal)}{Chemical Purity, % expressed as a decimal}$$

Solution Feeder Setting, gpd =
$$\frac{(Dose, mg/L)(Flow, MGD)(8.34 lb/gal)}{Solution Concentration, lb/gal}$$

Specific Gravity =
$$\frac{\text{Density of substance, lb/gal}}{8.34 \text{ lb/gal}}$$

Distribution Systems Calculations

Force*, lbs = (Pressure,psi)(Area, in²)

Leakage, gpd =
$$\frac{\text{Volume, gal}}{\text{Time, days}}$$

Slope,
$$\% = \frac{\text{Drop or Rise, ft}}{\text{Distance, ft}} \times 100\%$$

Water Use,
$$gpcd = \frac{Volume \text{ of Water Produced, } gpd}{Population Served, capita}$$

Alkalinity Relationships

All Alkalinity expressed as mg/L as CaCO₃ • P – phenolphthalein alkalinity • T – total alkalinity

Titration Results	Hydroxide	Carbonate	Bicarbonate
P = 0	0	0	Т
P is less than ½ T	0	(2)(P)	T – (2)(P)
P = ½ T	0	(2)(P)	0
P is greater than ½ T	(2)(P) – T	(2)(T) – (2)(P)	0
P = T	Т	0	0

^{*}Pie Wheel Format for this equation is available at the end of this document

Laboratory Calculations

Average (arithmetic mean) = $\frac{\text{Sum of All Terms}}{\text{Number of Terms}}$

Average (geometric mean) = $[(x_1)(x_2)(x_3)(x_4)...(x_n)]^{1/n}$

The nth root of the product of n numbers

Composite Sample Single Portion = $\frac{\text{(Instantaneous Flow)(Total Sample Volume)}}{\text{(Number of Portions)(Average Flow)}}$

Langelier Saturation Index = pH - pH_s

Specific Gravity =
$$\frac{\text{Density of substance, lb/gal}}{8.34 \text{ lb/gal}}$$

Threshold Odor Number = $\frac{(A+B)}{A}$

Where A = Volume of odor causing sample, and B = volume of odor free water

Chemistry

Milliequivalent = (mL)(Normality)

$$Molarity = \frac{Moles of Solute}{Liters of Solution}$$

Normality =
$$\frac{\text{Number of Equivalent Weights}}{\text{Liters of Solution}}$$

Number of Equivalent Weights =
$$\frac{\text{Total Weight}}{\text{Equivalent Weight}}$$

Number of Moles =
$$\frac{\text{Total Weight}}{\text{Molecular Weight}}$$

Temperature

Temperature, °C =
$$\frac{(°F-32)}{1.8}$$

Temperature, $^{\circ}F = (^{\circ}C)(1.8) + 32$

Titrations

Alkalinity, mg/L as
$$CaCO_3 = \frac{(Titrant\ Volume,\ mL)(0.02\ N)(50,000)}{Sample\ Volume,\ mL}$$

Hardness, mg/L as
$$CaCO_3 = \frac{(Titrant\ Volume,\ mL)(1,000)}{Sample\ Volume,\ mL}$$

Only when the titration factor is 1.00 of EDTA

Two Normal Equation $(C_1)(V_1)=(C_2)(V_2)$

Where C = Concentration or Normality and V = Volume Units must be compatible

Common Abbreviations

ac-ft = acre-feet

°C = Celsius

cfs = cubic feet per second

cm = centimeters

DO = dissolved oxygen

Eff = efficiency

EMF = electromotive force

°F = Fahrenheit

ft = feet

ft lb = foot-pound

g = grams

gal = gallons

gfd = gallons flux per day

gpcd = gallons per capita per day

gpd = gallons per day

gpg = grains per gallon

gpm = gallons per minute

HLR = hydraulic loading rate

hp = horsepower

hr = hours

in = inches

kg = kilograms

km = kilometers

kPa = kilopascals

kW = kilowatts

kWh = kilowatt-hours

L = liter

lb = pounds

LSI = Langelier Saturation Index

m = meters

mg = milligrams

MG = million gallons

MGD = million gallons per day

mi = miles

min = minutes

mL = milliliters

ppb = parts per billion

ppm = parts per million

psi = pounds per square inch

Q = flow

RPM = revolutions per minute

SDI = sludge density index

sec = second

SS = settleable solids

TOC = total organic carbon

TSS = total suspended solids

W = watts

WOR = weir overflow rate

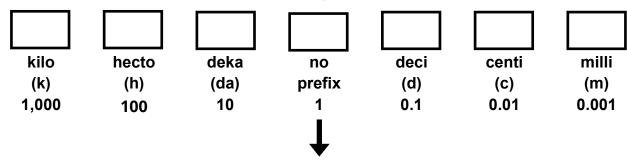
yd = yards

yr = year

Unit Conversion Factors

Weight and Mass Linear $1 \text{ ft}^3 \text{ of water} = 62.4 \text{ lb}$ 1 ft = 0.305 m1 ft = 12 in 1 g = 1,000 mg1 in = 2.54 cm1 gal of water = 8.34 lb 1 yd = 3 ft1 kg = 1,000 g1 mi = 5,280 ft1 kg = 2.2 lbs1 lb = 0.454 kgArea $1 \text{ ac} = 43,560 \text{ ft}^2$ 1 lb = 453.6 g1 ac = 0.405 Hectare1 metric ton = 2,205 lb $1 \text{ m}^2 = 1.19 \text{ yd}^2$ 1 mg/L = 0.0584 gpg $1 \text{ ft}^2 = 144 \text{ in}^2$ 1 gpg = 17.118 mg/L1 Hectare = 2.47 ac1 ton = 2,000 lb π or pi = 3.14 1% = 10,000 mg/LVolume **Pressure and Head** $1 \text{ ac-ft} = 43,560 \text{ ft}^3$ 1 atm = 33.9 ft of water1 ac-ft = 325,828.8 gal 1 atm = 14.7 psi $1 \text{ ft}^3 = 7.48 \text{ gal}$ 1 ft of water = 0.433 psi 1 L = 0.2642 gal1 psi = 2.31 ft of water 1 L = 1,000 mL**Power** $1 \text{ gal} = 231 \text{ in}^3$ 1 hp = 0.746 kW $1 \text{ gal} = 0.1337 \text{ ft}^3$ 1 hp = 746 W1 gal = 3.785 L1 hp = 33,000 ft•lb/min 1 MG = 1,000,000 gal 1 kW = 1,000 W $1 \text{ m}^3 = 264 \text{ gal}$ $1 \text{ vd}^3 = 27 \text{ ft}^3$ **Flow** 1 cfs = 0.6463 MGD 1 cfs = 448.8 gpm1 MGD = 694.44 gpm

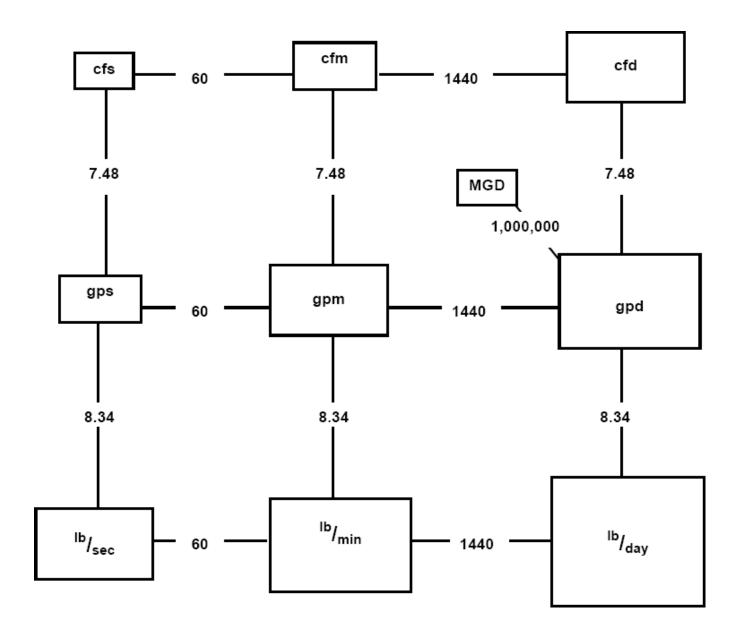
Metric Conversion Chart Primary Unit



meter (m) - linear measurement liter (L) - volume measurement gram (g) - weight measurement

1 MGD = 1.55 cfs

Flow Conversion Chart



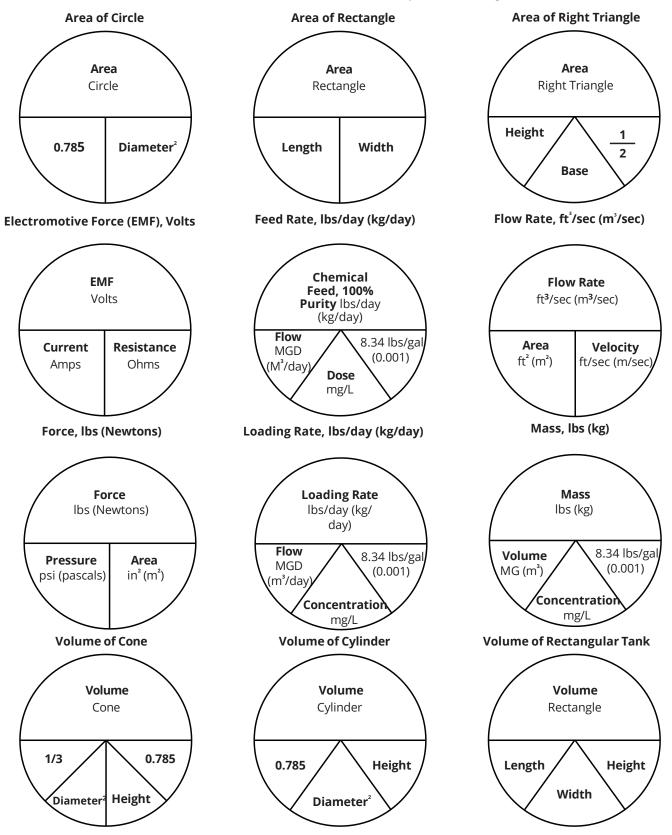
<u>To use this diagram</u>: First, find the box that coincides with the beginning units (i.e. gpm). Then, find the box that coincides with the desired ending units (i.e. cfs). The numbers between the starting point and ending point are the conversion factors.

When moving from a **smaller box to a larger box, multiply** by the factor between them.

When moving from a **larger box to a smaller box**, **divide** by the factor between them.

Pie Wheels

- To find the quantity above the horizontal line: multiply the pie wedges below the line together.
- To solve for one of the pie wedges below the horizontal line: cover that pie wedge, then divide the remaining pie wedge(s) into the quantity above the horizontal line.
- Given units must match the units shown in the pie wheel.
- When US and metric units or values differ, the metric is shown in parentheses, e.g. (m²).



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