



Department of
**Environment &
Conservation**



Tennessee Operator Certification Formula Manual

Collection Systems Formulas & Conversions

Prepared by the Fleming Training Center



About This Manual

This publication is provided by the Tennessee Department of Environment and Conservation (TDEC), Division of Water Resources (DWR), as an official resource for examinees participating in the State of Tennessee's operator certification program. It may be used during certification exams and is intended to support operators in understanding and applying essential mathematical formulas and conversions in the field.

This manual was collaboratively developed and reviewed by:

- **Fleming Training Center (FTC)** – content development and formatting
- **Water Professionals International (WPI)** – foundational formula reference materials
- **Tennessee Association of Utility Districts (TAUD)** – editorial review and industry input

This resource is intended to reflect Tennessee's commitment to operator preparedness and professional excellence. While based on national standards, the formatting and presentation have been tailored to meet the needs of Tennessee operators and exam settings.

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Circumference and Perimeter

Circumference of a Circle = $(3.14)(\text{Diameter})$

Perimeter, ft = $(2)(\text{Length, ft}) + (2)(\text{Width, ft})$

Area

Area of a Circle*, $\text{ft}^2 = (0.785)(\text{Diameter, ft})^2$

Area of a Circle, $\text{ft}^2 = (3.14)(\text{Radius, ft})^2$

Lateral Surface Area of a Cone, $\text{ft}^2 = (3.14)(\text{Radius, ft}) \left(\sqrt{(\text{Radius, ft})^2 + (\text{Height, ft})^2} \right)$

Total Surface Area of a Cone, $\text{ft}^2 = (3.14)(\text{Radius, ft}) \left(\text{Radius, ft} + \sqrt{(\text{Radius, ft})^2 + (\text{Height, ft})^2} \right)$

Total Exterior Surface Area of a Cylinder, $\text{ft}^2 =$
 $(\text{end \#1 SA, ft}^2) + (\text{end \#2 SA, ft}^2) + [(3.14)(\text{Diameter, ft})(\text{Height, ft})]$
Where SA = Surface Area

Area of a Rectangle*, $\text{ft}^2 = (\text{Length, ft})(\text{Width, ft})$

Area of a Right Triangle*, $\text{ft}^2 = \frac{[(\text{Base, ft})(\text{Height, ft})]}{2}$

Volume

Volume of a Cone*, $\text{ft}^3 = (1/3)(0.785)(\text{Diameter, ft})^2(\text{Height, ft})$

Volume of a Cylinder*, $\text{ft}^3 = (0.785)(\text{Diameter, ft})^2(\text{Height, ft})$

Volume of a Rectangular Tank*, $\text{ft}^3 = (\text{Length, ft})(\text{Width, ft})(\text{Height, ft})$

Volume, gallons = $(\text{Volume, ft}^3) (7.48 \text{ gal/ft}^3)$

Velocity and Flow

Velocity, ft/sec = $\frac{\text{Distance, ft}}{\text{Time, sec}}$

Flow*, $\text{ft}^3/\text{sec} = (\text{Area, ft}^2) (\text{Velocity, ft/sec})$

Flow Through a Channel, $\text{ft}^3/\text{sec} = (\text{Width, ft})(\text{Depth, ft})(\text{Velocity, ft/sec})$

Flow Through a Full Pipe, $\text{ft}^3/\text{sec} = (0.785)(\text{Diameter, ft})^2(\text{Velocity, ft/sec})$

Flow Through a Partially Full Pipe, $\text{ft}^3/\text{sec} = (\text{Factor from d/D table})(\text{Diameter, ft})^2(\text{Velocity, ft/sec})$
See pg. 12 for depth/Diameter Table

*Pie Wheel Format for this equation is available at the end of this document

Pounds (Feed Rate)

$$\text{Mass}^*, \text{ lb} = (\text{Concentration, mg/L})(\text{Volume, MG})(8.34 \text{ lb/gal})$$

$$\text{Mass, lb} = \frac{(\text{Concentration, mg/L})(\text{Volume, MG})(8.34 \text{ lb/gal})}{\text{Chemical Purity, \% as a decimal}}$$

$$\text{Loading Rate}^*, \text{ lb/day} = (\text{Concentration, mg/L})(\text{Flow, MGD})(8.34 \text{ lb/gal})$$

$$\text{Feed Rate, lb/day} = \frac{(\text{Dosage, mg/L})(\text{Flow, MGD})(8.34 \text{ lb/gal})}{\text{Chemical Purity, \% as a decimal}}$$

Dosage

$$\text{Dosage, mg/L} = \frac{(\text{Feed Rate, lb/day})}{(\text{Flow, MGD})(8.34 \text{ lb/gal})}$$

$$\text{Dosage, mg/L} = \frac{(\text{Feed Rate, lb/day})(\text{Chemical Purity, \% as a decimal})}{(\text{Flow, MGD})(8.34 \text{ lb/gal})}$$

$$\text{Dosage, mg/L} = \frac{(\text{Feed Mass, lb})(\text{Chemical Purity, \% as a decimal})}{(\text{Volume, MG})(8.34 \text{ lb/gal})}$$

Power

$$\text{Amps} = \frac{\text{Volts}}{\text{Ohms}}$$

$$\text{Amps (Single-Phase)} = \frac{(746 \text{ watts/HP})(\text{Horsepower})}{(\text{Volts})(\text{Efficiency, \% as a decimal})(\text{Power Factor})}$$

$$\text{Amps (Three-Phase)} = \frac{(746 \text{ watts/HP})(\text{Horsepower})}{(1.732)(\text{Volts})(\text{Efficiency, \% as a decimal})(\text{Power Factor})}$$

$$\text{Cost, \$/hour} = (\text{Motor Horsepower, hp})(0.746 \text{ kW/hp})(\text{Cost, \$/kW-hr})$$

$$\text{Electromotive Force}^*, \text{ volts} = (\text{Current, amps})(\text{Resistance, ohms})$$

$$\text{Horsepower} = \frac{(\text{EMF, volts})(\text{Amperage, amps})}{(746 \text{ watts/HP})}$$

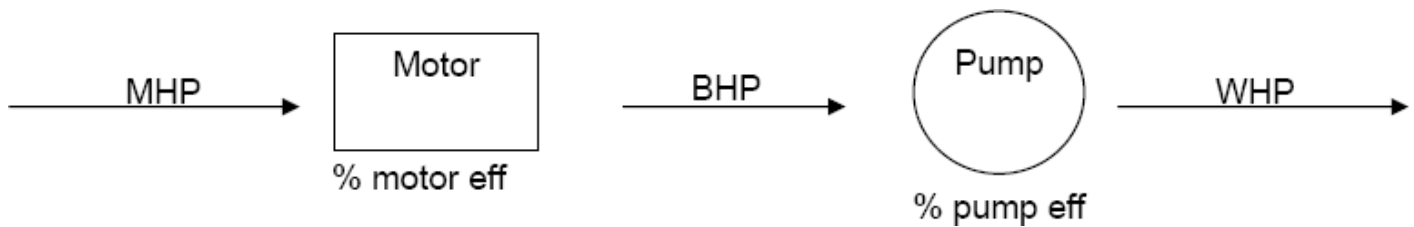
$$\text{Power, watts (AC Circuit)} = (\text{Volts})(\text{Amps})(\text{Power Factor})$$

$$\text{Power, watts (DC Circuit)} = (\text{Volts})(\text{Amps})$$

$$\text{Power Factor} = \frac{\text{Power, watts}}{(\text{EMF, volts})(\text{Amperage, amps})}$$

*Pie Wheel Format for this equation is available at the end of this document

Pumps and Motors



$$\text{Cycle Time, min} = \frac{\text{Storage Volume, gal}}{(\text{Pump Capacity, gpm} - \text{Wet Well Inflow, gpm})}$$

Horsepower

$$\text{Water Horsepower, hp} = \frac{(\text{Flow, gpm})(\text{Head, ft})}{(3,960)}$$

$$\text{Brake Horsepower, hp} = \frac{(\text{Flow, gpm})(\text{Head, ft})}{(3,960)(\text{Pump Efficiency, \% as a decimal})}$$

$$\text{Brake Horsepower, hp} = \frac{\text{Water Horsepower, hp}}{\text{Pump Efficiency, \% as a decimal}}$$

$$\text{Motor Horsepower, hp} = \frac{(\text{Flow, gpm})(\text{Head, ft})}{(3,960)(\text{Pump Efficiency, \% as a decimal})(\text{Motor Efficiency, \% as a decimal})}$$

$$\text{Motor Horsepower, hp} = \frac{\text{Water Horsepower, hp}}{(\text{Pump Efficiency, \% as a decimal})(\text{Motor Efficiency, \% as a decimal})}$$

$$\text{Motor Horsepower, hp} = \frac{\text{Brake Horsepower, hp}}{\text{Motor Efficiency, \% as a decimal}}$$

Efficiency

$$\text{Efficiency, \%} = \frac{\text{Horsepower Output, hp}}{\text{Horsepower Supplied, hp}} \times 100\%$$

$$\text{Pump Efficiency, \%} = \frac{\text{Water Horsepower, hp}}{\text{Brake Horsepower, hp}} \times 100\%$$

$$\text{Motor Efficiency, \%} = \frac{\text{Brake Horsepower, hp}}{\text{Motor Horsepower, hp}} \times 100\%$$

$$\text{Wire-to-Water Efficiency, \%} = (\text{Pump Efficiency, \% as a decimal})(\text{Motor Efficiency, \% as a decimal})(100\%)$$

$$\text{Wire-to-Water Efficiency, \%} = \frac{\text{Water Horsepower, hp}}{\text{Motor Horsepower, hp}} \times 100\%$$

$$\text{Wire-to-Water Efficiency, \%} = \frac{(\text{Flow, gpm})(\text{Total Dynamic Head, ft})(0.746 \text{ kW/hp})}{(3,960)(\text{Electrical Demand, kW})} \times 100\%$$

Pumps and Motors (continued)

Pumping Rate

$$\text{Pumping Rate, gpm} = \frac{\text{Volume, gal}}{\text{Time, min}}$$

$$\text{Pumping Rate of a Rectangular Tank, gpm} = \frac{(\text{Length, ft})(\text{Width, ft})(\text{Depth, ft})(7.48 \text{ gal/ft}^3)}{\text{Time, min}}$$

$$\text{Pumping Rate of a Cylindrical Tank, gpm} = \frac{(0.785)(\text{Diameter, ft})^2(\text{Depth, ft})(7.48 \text{ gal/ft}^3)}{\text{Time, min}}$$

$$\text{Time to Fill, min} = \frac{\text{Tank Volume, gal}}{\text{Flow Rate, gal/min}}$$

Collection Systems Calculations

$$\text{Average} = \frac{(\text{Time \#1} + \text{Time \#2})}{2}$$

$$\text{Blower Capacity, ft}^3/\text{min} = \frac{(0.785)(\text{Manhole Diameter, ft})^2(\text{Manhole Depth, ft})}{\text{Time for Air Change, min}}$$

$$\text{Slope, \%} = \frac{\text{Drop or Rise, ft}}{\text{Distance, ft}} \times 100\%$$

Force

$$\text{Force*}, \text{ lbs} = (\text{Pressure, psi})(\text{Area, in}^2)$$

$$\text{Force (cylinder), lbs} = (\text{Pressure, psi})(0.785)(\text{Diameter, in})^2$$

$$\text{Force (rectangle), lb} = (\text{Pressure, psi})(\text{Length, in})(\text{Width, in})$$

Leak Testing

$$\text{Leakage, gal} = (0.785)(\text{Manhole Diameter, ft})^2(\text{Water Drop, ft})(7.48 \text{ gal/ft}^3)$$

$$\text{Leakage, gal/day} = \frac{\text{Volume, gal}}{\text{Time, days}}$$

$$\text{Leakage, gal/hr} = \frac{\text{Leakage, gpd}}{24 \text{ hr/day}}$$

$$\text{Leakage, gal/day/inch} = \frac{\text{Leakage, gpd}}{\text{Sewer Diameter, in}}$$

$$\text{Leakage, gpd/inch/mile} = \frac{(\text{Leakage, gpd/in})(5280 \text{ ft/mi})}{\text{Pipe Length, ft}}$$

*Pie Wheel Format for this equation is available at the end of this document

Chlorination

Chlorine Dose, mg/L = Chlorine Demand, mg/L + Chlorine Residual, mg/L

Chlorine Demand, mg/L = Chlorine Dose, mg/L - Chlorine Residual, mg/L

Dosage, mg/L = $\frac{(\text{Feed Rate, lb/day})(\text{Chemical Purity, \% as a decimal})}{(\text{Flow, MGD})(8.34 \text{ lb/gal})}$

Feed Rate, lb/day = $\frac{(\text{Dosage, mg/L})(\text{Flow, MGD})(8.34 \text{ lb/gal})}{\text{Chemical Purity, \% as a decimal}}$

Chemical Feeders

Chemical, lbs = $\frac{(\text{Water Volume, gal})(8.34 \text{ lb/gal})(\text{Desired Concentration, \%})}{(100\% - \text{desired concentration, \%})}$

All percentages (%) should be entered in decimal form.

Water Volume, gal = $\frac{(\text{Chemical, lbs})(100\% - \text{Desired Concentration, \%})}{(\text{Desired Concentration, \%})(8.34 \text{ lb/gal})}$

Chemical Feed Pump Setting, % stroke = $\frac{\text{Desired flow}}{\text{Maximum flow}} \times 100\%$

Chemical Feed Pump Setting, mL/min = $\frac{(\text{Flow, MGD})(\text{Dose, mg/L})(3.785 \text{ L/gal})(1,000,000 \text{ gal/MG})}{(\text{Chemical Density, mg/mL})(\text{Active Chemical, \% as a decimal})(1440 \text{ min/day})}$

Dosage, mg/L = $\frac{(\text{Feed Rate, lb/day})(\text{Chemical Purity, \% as decimal})}{(\text{Flow, MGD})(8.34 \text{ lb/gal})}$

Feed Rate, lb/day = $\frac{(\text{Dosage, mg/L})(\text{Flow, MGD})(8.34 \text{ lb/gal})}{\text{Chemical Purity, \% as a decimal}}$

Solution Feeder Setting, gpd = $\frac{(\text{Dose, mg/L})(\text{Flow, MGD})(8.34 \text{ lb/gal})}{\text{Solution Concentration, lb/gal}}$

Laboratory Calculations

$$\text{Average (arithmetic mean)} = \frac{\text{Sum of All Terms}}{\text{Number of Terms}}$$

$$\text{Composite Sample Single Portion} = \frac{(\text{Instantaneous Flow})(\text{Total Sample Volume})}{(\text{Number of Portions})(\text{Average Flow})}$$

$$\text{Specific Gravity} = \frac{\text{Density of substance, lb/gal}}{8.34 \text{ lb/gal}}$$

Solution Preparation

$$\text{Three Normal Equation} = (C_1 \times V_1) + (C_2 \times V_2) = (C_3 \times V_3)$$

$$\text{Two Normal Equation} = (\text{Dilution}) (C_1 \times V_1) = (C_2 \times V_2)$$

*Where C = Concentration or Normality
and V = Volume*

Units must be compatible

Temperature

$$\text{Temperature, } ^\circ\text{C} = \frac{(^{\circ}\text{F} - 32)}{1.8}$$

$$\text{Temperature, } ^\circ\text{F} = (^{\circ}\text{C})(1.8) + 32$$

Collection Systems Formulas & Conversions

Common Abbreviations

| | |
|--|---|
| ac-ft = acre-feet | mg = milligrams |
| atm = atmospheres | MGD = million gallons per day |
| BOD ₅ = biochemical oxygen demand | mi = mile |
| °C = Celsius | mL = milliliters |
| CBOD ₅ = carbonaceous biochemical oxygen demand | MLSS = mixed liquor suspended solids |
| CCSS = clarifier core suspended solids | MLVSS = mixed liquor volatile suspended solids |
| cfs = cubic feet per second | OCR = oxygen consumption rate |
| cm = centimeters | OUR = oxygen uptake rate |
| COD = chemical oxygen demand | PE = population equivalent |
| DO = dissolved oxygen | ppb = parts per billion |
| EMF = electromotive force | ppm = parts per million |
| °F = Fahrenheit | psi = pounds per square inch |
| F/M Ratio = food to microorganism ratio | Q = flow |
| ft = feet | RAS = return activated sludge |
| ft lb = foot-pound | RBC = rotating biological contactor |
| g = grams | RPM = revolutions per minute |
| gal = gallons | SBOD ₅ = soluble BOD |
| gfd = gallons flux per day | SDI = sludge density index |
| gpcd = gallons per capita per day | sec = second |
| gpd = gallons per day | SOUR = specific oxygen uptake rate |
| gpg = grains per gallon | SRT = solids retention time |
| gpm = gallons per minute | SS = settleable solids |
| hp = horsepower | SSV ₃₀ = settled sludge volume 30 minute |
| hr = hours | SVI = sludge volume index |
| in = inches | TOC = total organic carbon |
| kg = kilograms | TS = total solids |
| km = kilometers | TSS = total suspended solids |
| kPa = kilopascals | VS = volatile solids |
| kW = kilowatts | VSS = volatile suspended solids |
| kWh = kilowatt-hours | W = watts |
| L = liter | WAS = waste activated sludge |
| lb = pounds | yd = yards |
| m = meters | yr = year |
| MCRT = mean cell residence time | |
| MG = million gallons | |

Unit Conversion Factors

Linear

1 ft = 0.305 m
1 ft = 12 in
1 in = 2.54 cm
1 yd = 3 ft
1 mi = 5,280 ft

Area

1 ac = 43,560 ft²
1 m² = 1.19 yd²
1 ft² = 144 in²
π or pi = 3.14

Volume

1 ac-ft = 43,560 ft³
1 ac-ft = 325,828.8 gal
1 ft³ = 7.48 gal
1 L = 0.2642 gal
1 L = 1,000 mL
1 gal = 231 in³
1 gal = 0.1337 ft³
1 gal = 3.785 L
1 MG = 1,000,000 gal
1 m³ = 264 gal
1 yd³ = 27 ft³

Flow

1 cfs = 0.6463 MGD
1 cfs = 448.8 gpm
1 MGD = 694.44 gpm
1 MGD = 1.55 cfs

Weight and Mass

1 ft³ of water = 62.4 lb
1 g = 1,000 mg
1 gal of water = 8.34 lb
1 kg = 1,000 g
1 kg = 2.2 lbs
1 lb = 0.454 kg
1 lb = 453.6 g
1 metric ton = 2,205 lb
1 mg/L = 0.0584 gpg
1 gpg = 17.118 mg/L
1 ton = 2,000 lb
1% = 10,000 mg/L

Pressure and Head

1 atm = 33.9 ft of water
1 atm = 14.7 psi
1 ft of water = 0.433 psi
1 psi = 2.31 ft of water
1 psi = 33,000 ft•lb/min

Power

1 hp = 0.746 kW
1 hp = 746 W
1 hp = 33,000 ft•lb/min
1 kW = 1,000 W

Population Equivalent

PE, hydraulic = 100 gal/person/day
PE, organic = 0.17 BOD/person/day

Metric Conversion Chart

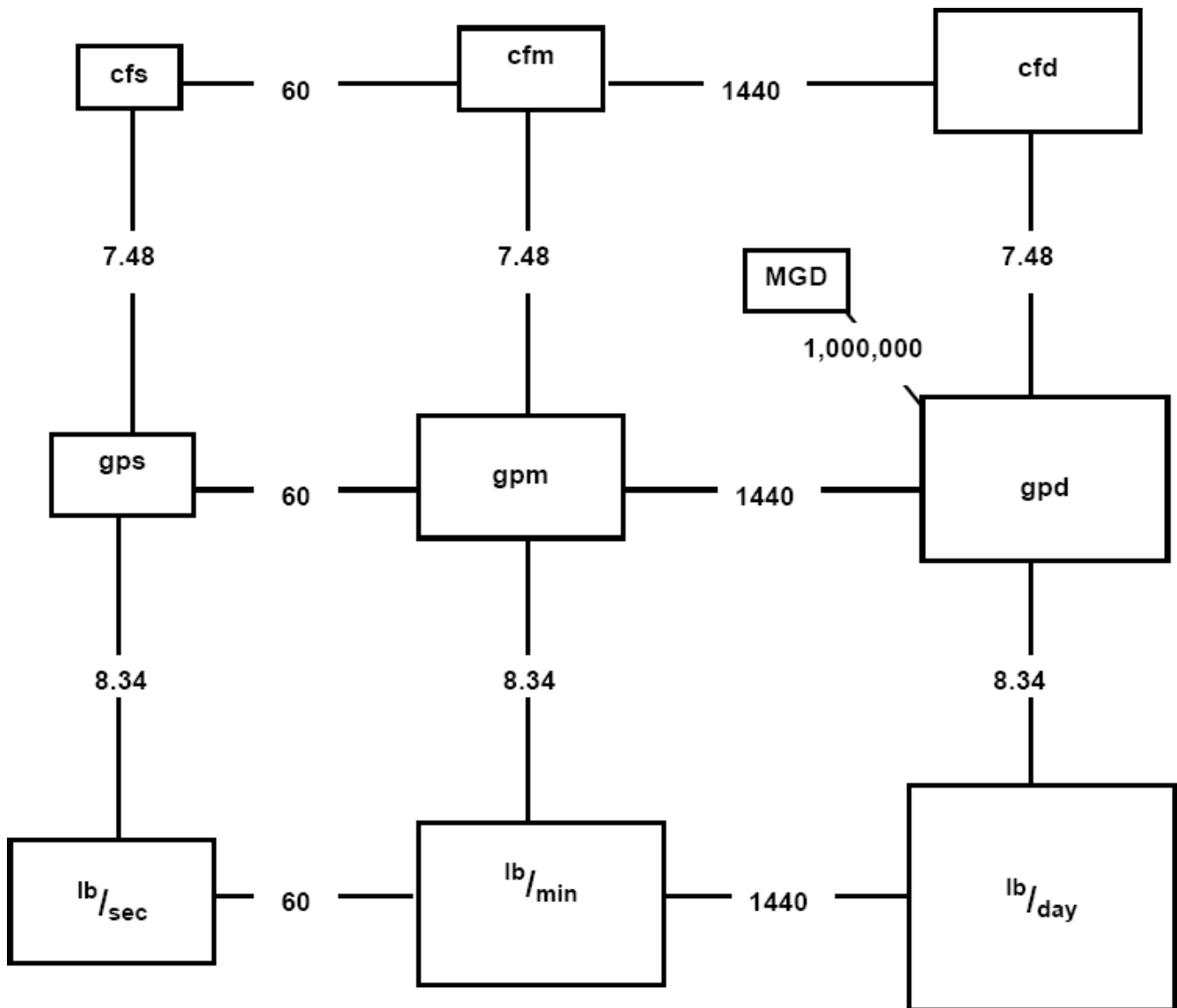
Primary Unit

| | | | | | | |
|----------------------|----------------------|----------------------|----------------------|----------------------|----------------------|----------------------|
| <input type="text"/> | <input type="text"/> | <input type="text"/> | <input type="text"/> | <input type="text"/> | <input type="text"/> | <input type="text"/> |
| kilo | hecto | deka | no | deci | centi | milli |
| (k) | (h) | (da) | prefix | (d) | (c) | (m) |
| 1,000 | 100 | 10 | 1 | 0.1 | 0.01 | 0.001 |



meter (m) - linear measurement
liter (L) - volume measurement
gram (g) - weight measurement

Flow Conversion Chart



To use this diagram: First, find the box that coincides with the beginning units (i.e. gpm). Then, find the box that coincides with the desired ending units (i.e. cfs). The numbers between the starting point and ending point are the conversion factors.

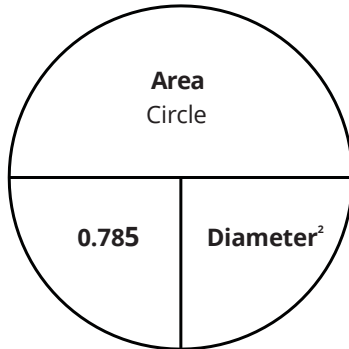
When moving from a **smaller box to a larger box, multiply** by the factor between them.

When moving from a **larger box to a smaller box, divide** by the factor between them.

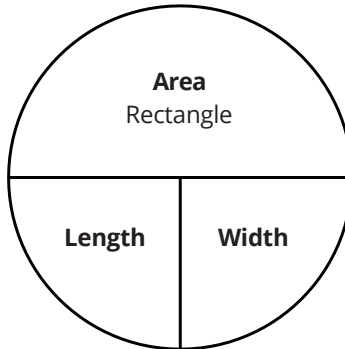
Pie Wheels

- To find the quantity above the horizontal line: multiply the pie wedges below the line together.
- To solve for one of the pie wedges below the horizontal line: cover that pie wedge, then divide the remaining pie wedge(s) into the quantity above the horizontal line.
- Given units must match the units shown in the pie wheel.
- When US and metric units or values differ, the metric is shown in parentheses, e.g. (m²).

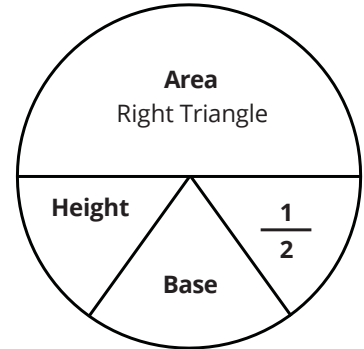
Area of Circle



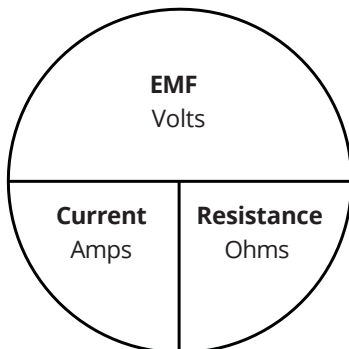
Area of Rectangle



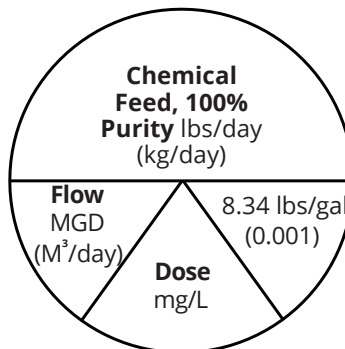
Area of Right Triangle



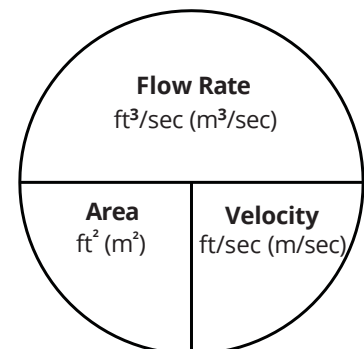
Electromotive Force (EMF), Volts



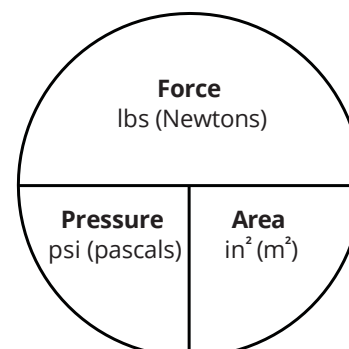
Feed Rate, lbs/day (kg/day)



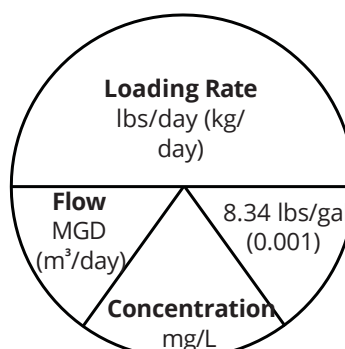
Flow Rate, ft³/sec (m³/sec)



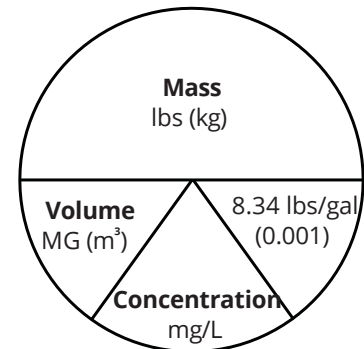
Force, lbs (Newtons)



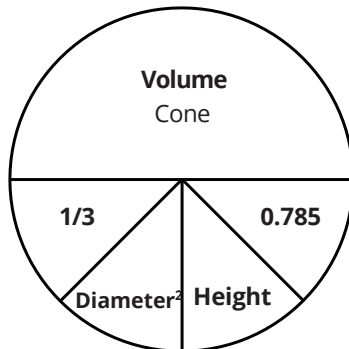
Loading Rate, lbs/day (kg/day)



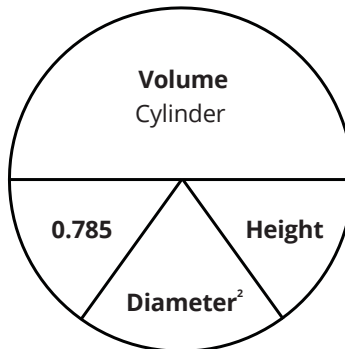
Mass, lbs (kg)



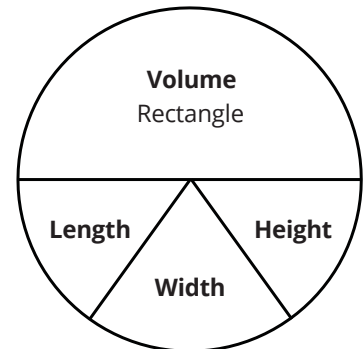
Volume of Cone



Volume of Cylinder



Volume of Rectangular Tank



Flow Through a Partially Full Pipe



Where D = diameter, and d = depth

$$\text{Flow, cfs} = (\text{Area, ft}^2)(\text{Velocity, fps})$$

$$\text{Flow, cfs} = [(\text{factor from } d/D \text{ table})(\text{Diameter, ft})^2](\text{Velocity, fps})$$

| d, in / D, in | Factor | d, in / D, in | Factor | d, in / D, in | Factor | d, in / D, in | Factor |
|---------------|--------|---------------|--------|---------------|--------|---------------|--------|
| 0.01 | 0.0013 | 0.26 | 0.1623 | 0.51 | 0.4027 | 0.76 | 0.6404 |
| 0.02 | 0.0037 | 0.27 | 0.1711 | 0.52 | 0.4127 | 0.77 | 0.6489 |
| 0.03 | 0.0069 | 0.28 | 0.1800 | 0.53 | 0.4227 | 0.78 | 0.6573 |
| 0.04 | 0.0105 | 0.29 | 0.1890 | 0.54 | 0.4327 | 0.79 | 0.6655 |
| 0.05 | 0.0147 | 0.30 | 0.1982 | 0.55 | 0.4426 | 0.80 | 0.6736 |
| 0.06 | 0.0192 | 0.31 | 0.2074 | 0.56 | 0.4526 | 0.81 | 0.6813 |
| 0.07 | 0.0242 | 0.32 | 0.2167 | 0.57 | 0.4625 | 0.82 | 0.6893 |
| 0.08 | 0.0294 | 0.33 | 0.2260 | 0.58 | 0.4724 | 0.83 | 0.6969 |
| 0.09 | 0.0350 | 0.34 | 0.2355 | 0.59 | 0.4822 | 0.84 | 0.7043 |
| 0.10 | 0.0409 | 0.35 | 0.2450 | 0.60 | 0.4920 | 0.85 | 0.7115 |
| 0.11 | 0.0470 | 0.36 | 0.2546 | 0.61 | 0.5018 | 0.86 | 0.7186 |
| 0.12 | 0.0534 | 0.37 | 0.2642 | 0.62 | 0.5118 | 0.87 | 0.7254 |
| 0.13 | 0.0600 | 0.38 | 0.2739 | 0.63 | 0.5212 | 0.88 | 0.7320 |
| 0.14 | 0.0668 | 0.39 | 0.2836 | 0.64 | 0.5308 | 0.89 | 0.7384 |
| 0.15 | 0.0739 | 0.40 | 0.2934 | 0.65 | 0.5404 | 0.90 | 0.7445 |
| 0.16 | 0.0811 | 0.41 | 0.3032 | 0.66 | 0.5499 | 0.91 | 0.7504 |
| 0.17 | 0.0885 | 0.42 | 0.3130 | 0.67 | 0.5594 | 0.92 | 0.7560 |
| 0.18 | 0.0961 | 0.43 | 0.3229 | 0.68 | 0.5687 | 0.93 | 0.7612 |
| 0.19 | 0.1039 | 0.44 | 0.3328 | 0.69 | 0.5780 | 0.94 | 0.7662 |
| 0.20 | 0.1118 | 0.45 | 0.3428 | 0.70 | 0.5872 | 0.95 | 0.7707 |
| 0.21 | 0.1199 | 0.46 | 0.3527 | 0.71 | 0.5964 | 0.96 | 0.7749 |
| 0.22 | 0.1281 | 0.47 | 0.3627 | 0.72 | 0.6054 | 0.97 | 0.7785 |
| 0.23 | 0.1365 | 0.48 | 0.3727 | 0.73 | 0.6143 | 0.98 | 0.7816 |
| 0.24 | 0.1449 | 0.49 | 0.3827 | 0.74 | 0.6231 | 0.99 | 0.7841 |
| 0.25 | 0.1535 | 0.50 | 0.3927 | 0.75 | 0.6318 | 1.00 | 0.7854 |