

Teacher Training on the Revised Math Standards

Grades 3–5



Welcome & Introductions

| Agenda | a: Day 1 |
|--------------------------------|--|
| Time | Content |
| 8–11:15 (includes break) | Part 1: The Standards M1: Standards Review Process M2: TN Academic Standards M3: Summary of Revisions |
| 11:15–12:30 | Lunch (on your own) |
| 12:30–4 (includes break) | Part 2: Diving into the Standards • M4: Know-Do-Understand Part 3: Instructional Shifts • M5: Revisiting SMP's and Instructional Shifts • M6: Literacy Skills for Mathematical Proficiency |
| TN Department of Education | |

| Time | Content |
|--------------------------------|---|
| 8–11:15 (includes break) | Part 4: Assessment • M7: Connecting Standards and Assessment |
| 11:15–12:30 | Lunch (on your own) |
| 12:30–4 (includes break) | M8: Evaluating Instructional Materials Part 5: Putting it All Together M9: Instructional Planning |

Norms

- Keep students at the center.
- Be present and engaged.
- Be reflective and solutions oriented.
- Challenge ideas with respect.
- Monitor airtime.



Introductions

- Make a name tent
 - Top left corner: # of ★ = how many years you have taught
 - Top right corner: where you're from
 - Bottom left corner: your favorite hobby
 - Bottom right corner: the name of a student who inspires you to learn and improve





Today's Goals

- Review the standards revision process.
- Highlight changes/revisions to standards.
- Use a KUD exercise to deepen our understanding of the expectations of the standards.
- Discuss the instructional shifts and their relationship to the Standards for Mathematical Practice (SMPs).
- Explore the Literacy Skills for Mathematical Proficiency.

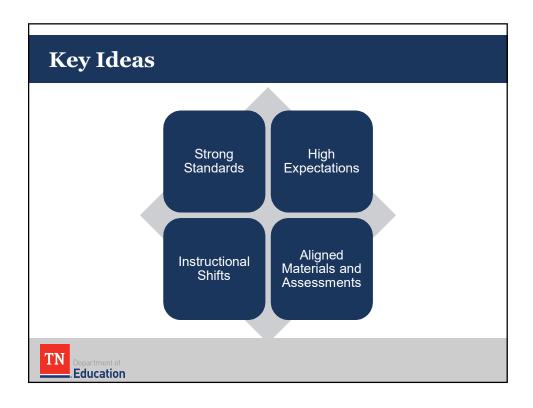


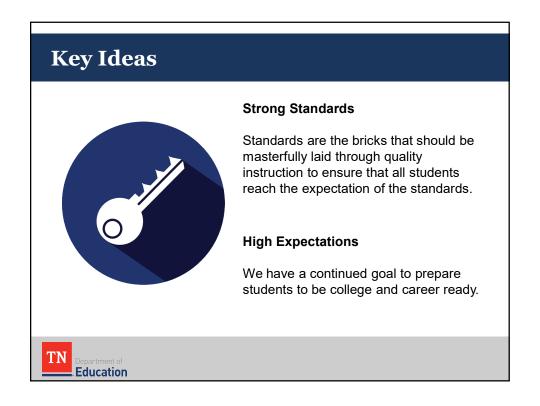
Appointment with Peers

- Create an appointment with four fellow participants by having them sign your manual.
- Participant partners will meet together during the training to discuss content.









Key Ideas



Instructional Shifts

The instructional shifts are an essential component of the standards and provide guidance for how the standards should be taught and implemented.

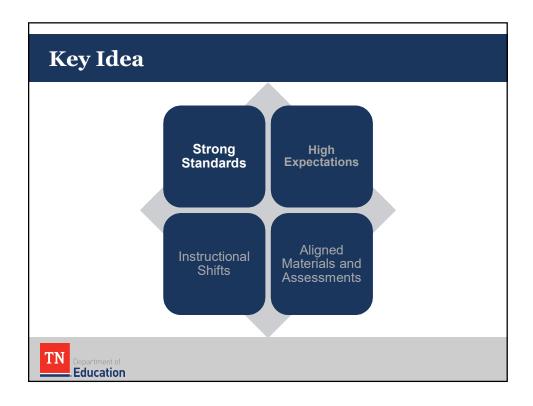
Aligned Materials and Assessments

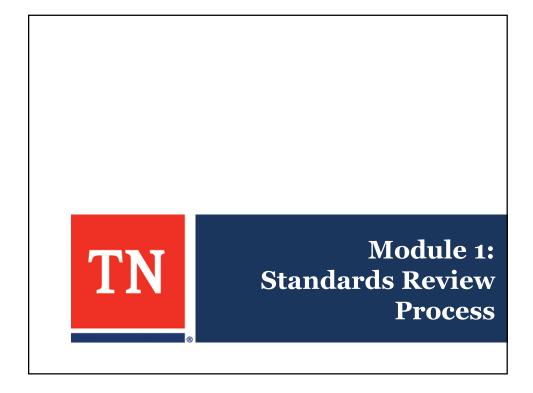
Educators play a key role in ensuring that our standards, classroom instructional materials and assessments are aligned.



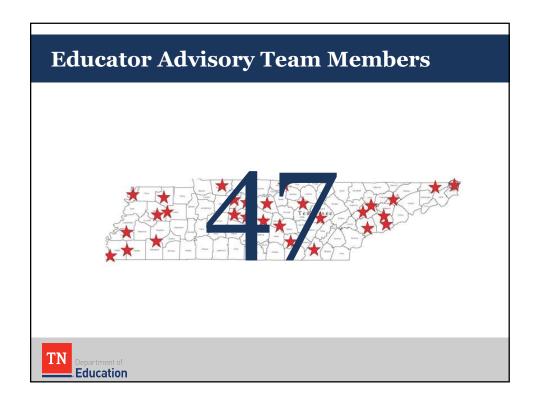


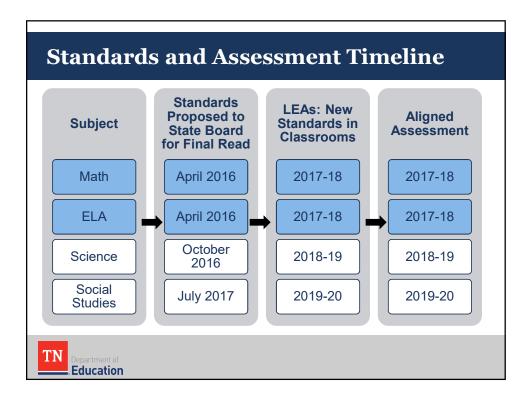
Part 1: The Standards











Standards Revision Key Points

- The instructional shifts remain the same and are still the focus of the standards.
- The revised standards represent a stronger foundation that will support the progression of rigorous standards throughout the grade levels.
- The revised standards improve connections:
 - within a single grade level, and
 - between multiple grade levels.





Module 2: Tennessee Academic Standards for Mathematics

Goals

- Reinforce the continued expectations of the Tennessee Math Academic Standards.
- Revisit the three instructional expectations and their continued and connected role in the current standards.
- Review the overarching changes to the current Tennessee Math Academic Standards.



Setting the Stage

- Read and annotate the General Introduction to the TN Math Standards (page 1–2).
- After reading and annotating the two parts, write the sentence or phrase you felt was the most important in your participant manual on page.
- Be prepared to share with your colleagues.





What Has **NOT** Changed

Overview of Similarities

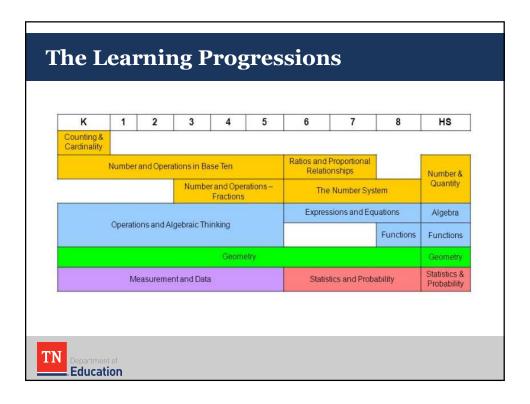
• Students **prepared** for college and career

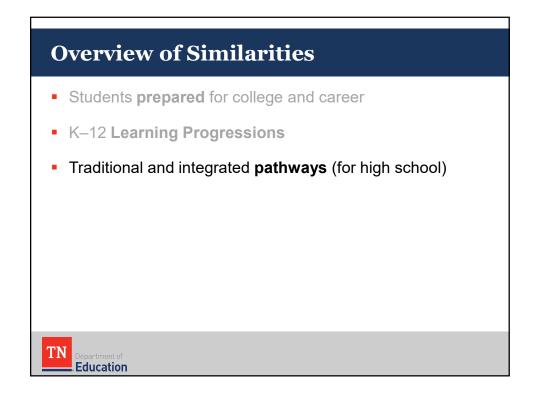


Overview of Similarities

- Students **prepared** for college and career
- K-12 learning progressions







Overview of Similarities

- Students prepared for college and career
- K-12 Learning Progressions
- Traditional and Integrated pathways
- Standards for Mathematical Practice



Standards for Mathematical Practice

Standards for Mathematical Practice

- 1. Make sense of problems and persevere in solving them.
- 2. Reason abstractly and quantitatively.
- 3. Construct viable arguments and critique the reasoning of others.
- 4. Model with mathematics.
- 5. Use appropriate tools strategically.
- Attend to precision.
- 7. Look for and make use of structure.
- 8. Look for and express regularity in repeated reasoning.



Overview of Similarities

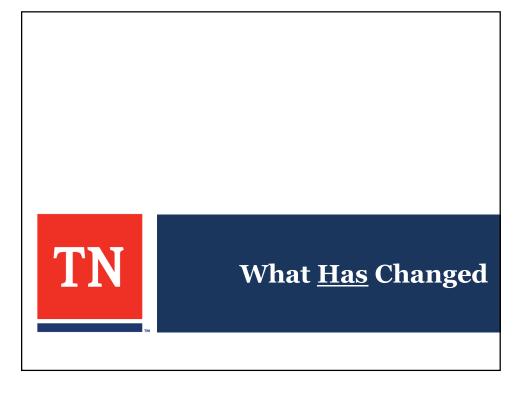
- Students prepared for college and career
- K-12 Learning Progressions
- Traditional and Integrated pathway
- Standards for Mathematical Practices
- Instructional shifts

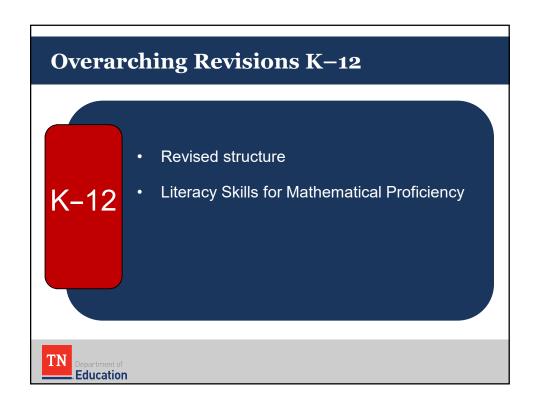


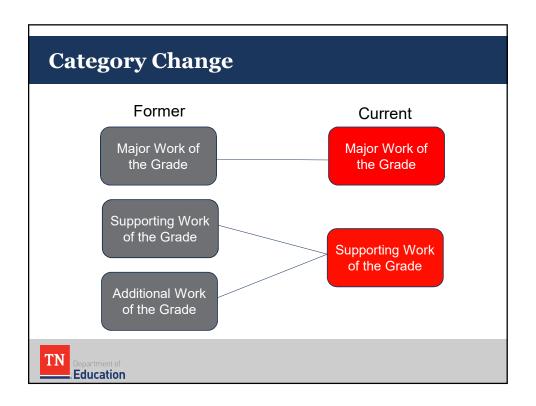
Instructional Shifts

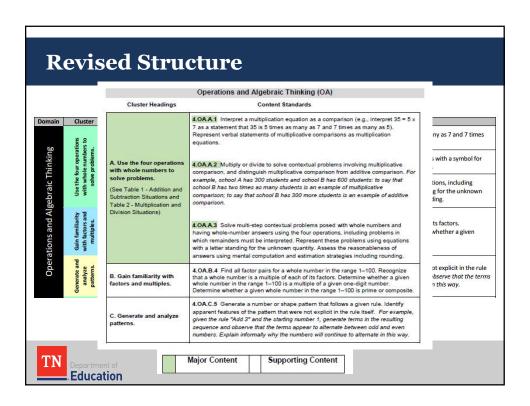
- Focus
 - The standards are focused on fewer topics so that students can dig deeper within the mathematics.
- Coherence
 - Topics within a grade are connected to support focus.
 Additionally, standards are linked across grades to ensure vertical coherence.
- Rigor
 - The standards set expectations for a balanced approach to pursuing conceptual understanding, procedural fluency, application, and modeling.

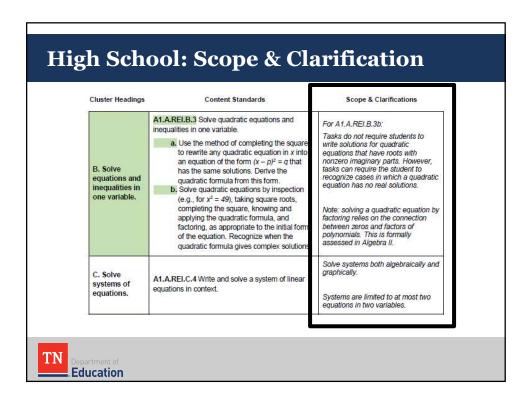


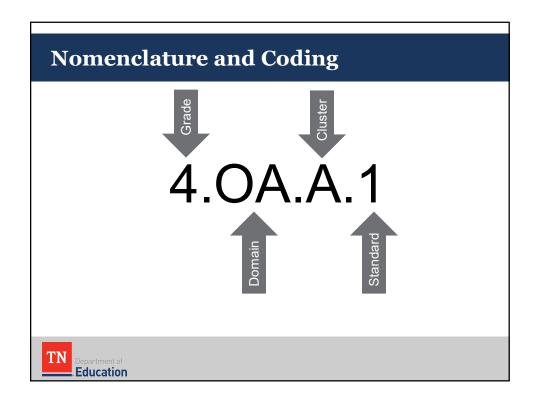












Literacy Skills for Mathematical Proficiency

Communication in mathematics requires literacy skills in reading, vocabulary, speaking, listening, and writing.

Literacy Skills for Mathematical Proficiency

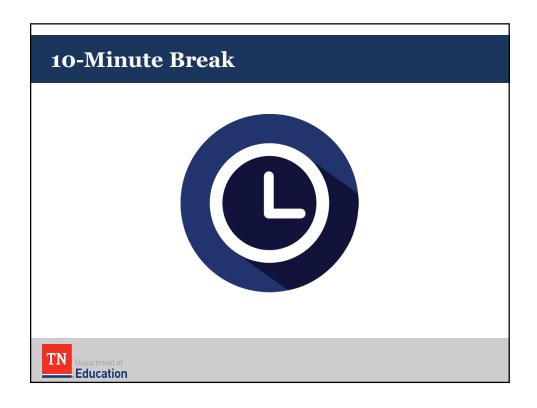
- 1. Use multiple reading strategies.
- 2. Understand and use correct mathematical vocabulary.
- Discuss and articulate mathematical ideas.
- 4. Write mathematical arguments.

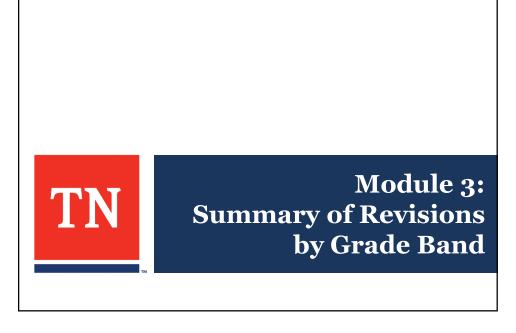


Module 2 Review

- Reinforce the continued expectations of the Tennessee Math Standards.
- Revisit the three instructional shifts and their continued and connected role in the revised standards.
- Review the overarching changes to the revised Tennessee Math Standards.







Goal

 Review a summary of the revisions to the math standards by grade band.

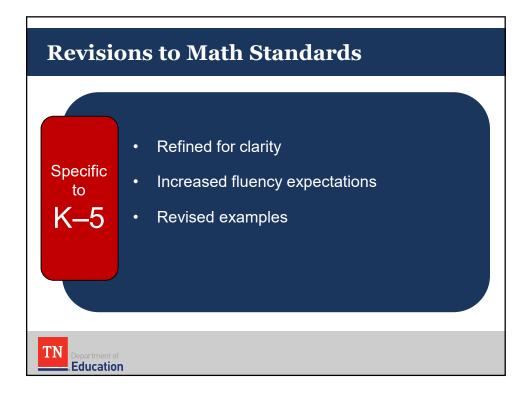


Turn & Talk

"To assess student achievement accurately, teachers and administrators must know and understand the content standards that their students are to master. Again, we cannot teach or assess achievement that we have not defined."

—S. Chappuis, Stiggins, Arter, and J. Chappuis, 2006





- Supporting and additional work of the grade is combined as supporting work of the grade
- Increased fluency expectations
- Added/shifted a small number of standards to strengthen coherence across grade levels
- Revised language to provide clarity and continuity
- Highlighted chart for grade-level mastery expectations for addition, subtraction, multiplication, and division



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Sample Revision: K-2

| | Increased Fluency Expectations | | |
|-----------------|--|--|--|
| | Former Standard | Current Standard | |
| Kindergarten | K. OA.5 Fluently add and subtract within <u>5</u> . | K.OA.A.5 Fluently add and subtract within <u>10</u> using mental strategies. | |
| First Grade | 1.OA.6. Add and subtract within <u>20</u> , demonstrating fluency for addition and subtraction within <u>10</u> . | 1.OA.C.6 Fluently add and subtract within <u>20</u> using mental strategies. By the end of Grade 1, know from memory all sums up to <u>10</u> . | |
| Second Grade | 2.OA.2 Fluently add and subtract within 20 using mental strategies. By end of Grade 2, know from memory all sums of two one-digit numbers. | 2.OA.B.2 Fluently add and subtract within 30 using mental strategies. By the end of Grade 2, know from memory all sums of two one-digit numbers and related subtraction facts. | |



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Education

Sample Revision: K-2 Former Standard **Current Standard** No Past Standard K.MD.B.3 Identify the penny, nickel, Kindergarten dime, and quarter and recognize the value of each. No Past Standard 1.MD.B.4 Count the value of a set of like First coins less than one dollar using the ¢ Grade symbol only. 2.MD.8 Solve word problems involving 2.MD.C.8 Solve contextual problems dollar bills, quarters, dimes, nickels, Second involving dollar bills, quarters, dimes, and pennies, using \$ and ¢ symbols Grade nickels, and pennies using ¢ and \$ appropriately. symbols appropriately.

| Sa | mple Revision: 3–5 | ; |
|-----------------|---|--|
| | Former Standard | Current Standard |
| Fourth Grade | in a larger and in terms of a emailer and. I teesta | 4.MD.A.1 Measure and estimate to determine relative sizes of measurement units within a single system of measurement involving length, liquid volume, and mass/weight of objects using customary and metric units. |
| Fifth Grade | 5.MD.1 Convert among different-sized standard measurement units within a given measurement system (e.g., convert 5 cm to 0.05 m), and use these conversions in solving multi-step, real world problems. | 5.MD.A.1 Convert customary and metric measurement units within a single system by expressing measurements of a larger unit in terms of a smaller unit. Use these conversions to solve multi-step real world problems involving distances, intervals of time, liquid volumes, masses of objects, and money (including problems involving simple fractions or decimals). For example, 3.6 liters and 4.1 liters can be combined as 7.7 liters or 7700 milliliters. |
| TN | Department of Education | |

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Sample Revision: K-2

Former Standard

2.NBT.3 Read and write numbers to 1000 using base-ten numerals, number names, and expanded form.

Current Standard

2.NBT.A.3 Read and write numbers to 1000 using **standard form**, **word form**, and expanded form.



Sample Revision: 3-5

Former Standard

4.NBT.3 Use place value understanding to round multi-digit whole numbers to any place.

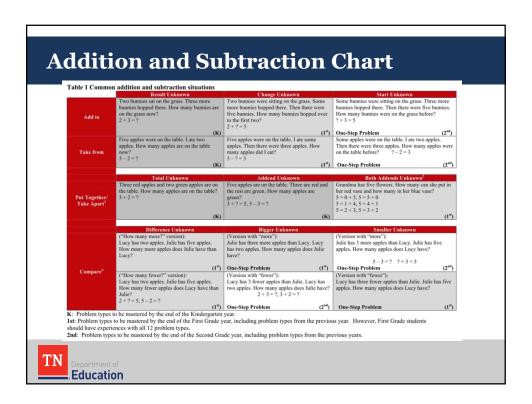
Current Standard

4.NBT.A.3 Round multi-digit whole numbers to any place (up to and including the hundred-thousand place) using understanding of place value.

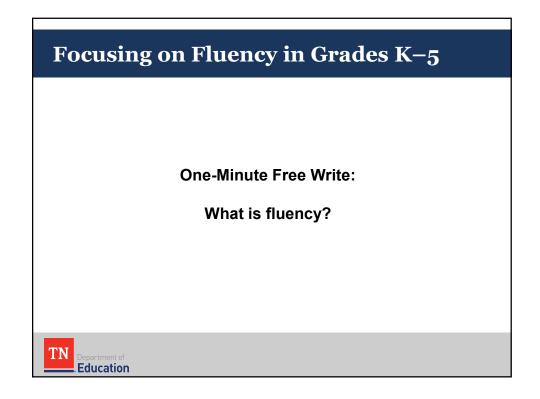


- Supporting and additional work of the grade is combined as supporting work of the grade
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| abic 2 Comi | non multiplication and division site Unknown Product | | | |
|----------------------|---|---|---|--|
| | 2002 (St. 1892) | Group Size Unknown ("How many in each group?" Division) | Number of Groups Unknown ("How many groups?" Division) | |
| | 3 × 6 = ? | $3 \times ? = 18$, and $18 \div 3 = ?$ | $? \times 6 = 18$, and $18 \div 6 = ?$ | |
| | There are 3 bags with 6 plums in each bag. How many plums are there in all? | If 18 plums are shared equally into 3 bags, then how many plums will be in each bag? | If 18 plums are to be packed 6 to a bag, then how many bags are needed? | |
| Equal Groups | Measurement example. You need 3 lengths of string, each 6 inches long. How much string will you need altogether? | Measurement example. You have 18 inches of string, which you will cut into 3 equal pieces. How long will each piece of string be? | Measurement example. You have 18 inches of string, which you will cut into pieces that are 6 inches long. How many pieces of string will you have? | |
| Arrays, ² | There are 3 rows of apples with 6 apples in each row. How many apples are there? | If 18 apples are arranged into 3 equal rows, how many apples will be in each row? Area example. A rectangle has area 18 | If 18 apples are arranged into equal rows of 6 apples, how many rows will there be? | |
| Area | Area example. What is the area of a 3 cm by 6 cm rectangle? | square centimeters. If one side is 3 cm long, how long is a side next to it? | Area example. A rectangle has area 18 square centimeters. If one side is 6 cm long, how long is a side next to it? | |
| | A blue hat costs \$6. A red hat costs 3 times as much as the blue hat. How much does the red hat cost? | A red hat costs \$18 and that is 3 times as much as a blue hat costs. How much does a blue hat cost? | A red hat costs \$18 and a blue hat costs \$6. How many times as much does the red hat cost as the blue hat? | |
| Compare | Measurement example. A rubber band is 6 cm long. How long will the rubber band be when it is stretched to be 3 times as long? | Measurement example. A rubber band is stretched to be 18 cm long and that is 3 times as long as it was at first. How long was the rubber band at first? | Measurement example. A rubber band was 6 cm long at first. Now it is stretched to be 18 cm long. How many times as long is the rubber band now a it was at first? | |



Fluency

"All students should be able to recall and use their math education when the need arises. That is, a student should know certain math facts and concepts such as the multiplication table, how to add, subtract, multiply, and divide basic numbers, how to work with simple fractions and percentages, etc. There is a level of procedural fluency that a student's K–12 math education should provide him or her along with conceptual understanding so that this can be recalled and used throughout his or her life."

-Tennessee Math Standards



What is Fluency?

- The ability to apply procedures <u>accurately</u>, <u>efficiently</u>, and <u>flexibly</u>
- Recognizing when one strategy or procedure is more appropriate to apply than another
- Having opportunities to justify both informal strategies and commonly used procedures through distributed practice
- Procedural fluency includes computational fluency with the four arithmetic operations. In the early grades, students are expected to develop fluency with whole numbers in addition, subtraction, multiplication, and division.



Definition of Fluency

Computational fluency refers to having **efficient and accurate methods** for computing. Students exhibit computational fluency when they demonstrate **flexibility** in the computational methods they choose, **understand** and **can explain** these methods, and **produce accurate answers efficiently**.

The computational **methods** that a student uses should be **based** on mathematical **ideas** that the student **understands well**, including the structure of the base-ten number system, properties of multiplication and division, and number relationships.



Fluency Progression Chart

Examine the fluency standards for each. How do the ideas build upon one another? Or, in other words, what is the vertical alignment?

| Focus | K | 1 | 2 | 3 | 4 | 5 |
|-------|---|---|---|---|---|---|
| | | | | | | |
| | | | | | | |
| | | | | | | |
| | | | | | | |



Fluency Standards: K-2

- K.OA.A.5 Fluently add and subtract within 10 using mental strategies.
- 1.OA.C.6 Fluently add and subtract within 20 using mental strategies. By the end of 1st grade, know from memory all sums up to 10.
- 2.OA.B.2 Fluently add and subtract within 30 using mental strategies. By the end of 2nd grade, know from memory all sums of two one-digit numbers and related subtraction facts.
- 2.NBT.B.5 Fluently add and subtract within 100 using properties of operations, strategies based on place value, and/or the relationship between addition and subtraction.



Fluency Standards: 3

- 3.OA.C.7 Fluently multiply and divide within 100, using strategies such as the relationship between multiplication and division (e.g., knowing that 8 x 5 = 40, one knows 40 ÷ 5 = 8) or properties of operations. By the end of 3rd grade, know from memory all products of two one-digit numbers and related division facts.
- 3.NBT.A.2 Fluently add and subtract within 1000 using strategies and algorithms based on place value, properties of operations, and/or the relationship between addition and subtraction.



Fluency Standards: 4-5

- 4.NBT.B.4 Fluently add and subtract within 1,000,000 using appropriate strategies and algorithms.
- 5.NBT.B.5 Fluently multiply multi-digit whole numbers (up to three-digit by four-digit factors) using appropriate strategies and algorithms.



| | Kindergarten | 1 st Grade | 2 nd Grade | 3 rd Grade | 4 th Grade | 5 th Grade |
|-------------------------|---|---|---|--|---|--|
| Fluency Expectations | Mental addition and subtraction within 10 | Mental addition and subtraction within 20 | Mental addition and subtraction within 30 | Addition and subtraction within 1000 using strategies, algorithms, properties, and relationships | Addition and subtraction within 1,000,000 using strategies and algorithms | Multiplication of multi-digit whole numbers (up to three-digit by four-digit factors) using strategies and algorithms |
| | | Memorization of all sums up to 10 | Addition and subtraction within 100 using properties, strategies, and relationships. | Memorization of all products of two one-digit numbers and related division facts | | |
| | | | Memorization of all sums of two one-digit numbers and related subtraction facts | Multiplication and division within 100 using strategies, relationships, or properties | | |

Strategies for Teaching Fluency

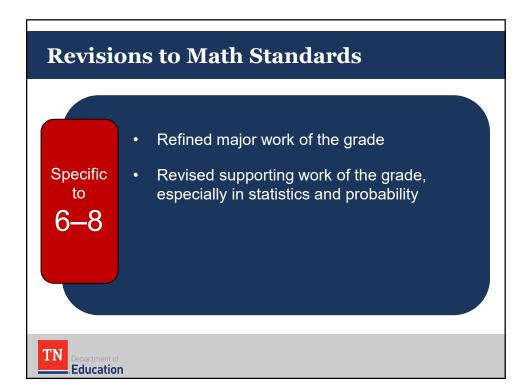
- Technology Use: use of technology such as mobile math apps have been shown to improve fluency (Shin, S., & Kwon, J., 2014, p. 1).
- Self-Management Techniques: Students who were taught self-management techniques such as asking questions like, "Am I paying attention?" were shown to have increased mathematical fluency (McDougall & Brady, 1998).
- (If you must use timed practice) Distributed, Rather than Explicit, Timed Practice: In a study on 3rd grade students in the Midwest, students gained more fluency with basic math facts when timed practice was distributed across the day rather than all at once.
- Games: Using games such as 24 can increase procedural fluency (Suh, J.).



References

- McDougall, D., & Brady, M. P. (1998). Initiating and fading self-management interventions to increase math fluency in general education classes. *Exceptional Children*, *64*(2), 151–166.
- National Research Council. (2001). Adding it up: Helping children learn mathematics. J. Kilpatrick, J. Swafford, and B. Findell (Eds.).
 Mathematics Learning Study Committee, Center for Education, Division of Behavioral and Social Sciences and Education. Washington, DC: National Academy Press.
- Principles and standards for school mathematics. (2000). Reston, VA: National Council of Teachers of Mathematics.
- Shin, S., & Kwon, J. (2014). Effect of mobile math applications on arithmetic fluency of underachieving students in math.
- Schutte, G. M., Duhon, G. J., Solomon, B. G., Poncy, B. C., Moore, K., & Story, B. (2015). A comparative analysis of massed vs. distributed practice on basic math fact fluency growth rates. *Journal of School Psychology*, 53(2), 149–159.
- Suh, J. (n.d.). The Five Strands of Mathematics. Retrieved from http://mason.gmu.edu/~jsuh4/teaching/procedure.htm





Grades 6–8: Overarching Revisions

- Slight revisions made to geometry in grade 8
- Supporting and additional work of the grade is combined as supporting work of the grade
- Revised language to provide clarity and continuity
- Revised a small number of standards to strengthen coherence by condensing, expanding, and removing standards
- Revised a small number of statistics and probability standards



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Grades 6–8: Sample Revision

Former Standard

6.SP.2 Understand that a set of data collected to answer a statistical question has a distribution which can be described by its center, spread, and overall shape.

Current Standard

6.SP.A.2 Understand that a set of data collected to answer a statistical question has a distribution which can be described by its center **(mean, median, mode)**, spread **(range)**, and overall shape.



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Grades 6–8: Sample Revision

Former Standard

6.EE.9 Use variables to represent two quantities in a real-world problem that change in relationship to one another. For example, Susan is putting money in her savings account by depositing a set amount each week (50). Represent her savings account balance with respect to the number of weekly deposits (s = 50w, illustrating the relationship between balance amount s and number of weeks w). Write an equation to express one quantity, thought of as the dependent variable, in terms of the other quantity, thought of as the independent variable. Analyze the relationship between the dependent and independent variables using graphs and tables, and relate these to the equation.



Grades 6–8: Sample Revision

Current Standard

6.EE.C.9 Use variables to represent two quantities in a real-world problem that change in relationship to one another. For example, Susan is putting money in her savings account by depositing a set amount each week (50). Represent her savings account balance with respect to the number of weekly deposits (s = 50w, illustrating the relationship between balance amount s and number of weeks w).

- **a.** Write an equation to express one quantity, thought of as the dependent variable, in terms of the other quantity, thought of as the independent variable.
- **b.** Analyze the relationship between the dependent and independent variables using graphs and tables, and relate these to the equation.



Grades 6–8: Sample Revision

Former Standard

7.G.A.3 Describe the two-dimensional figures that result from slicing three dimensional figures, as in plane sections of right rectangular prisms and right rectangular pyramids



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Grades 6–8: Sample Revision

Former Standard

6.SP.5c Summarize numerical data sets in relation to their context, such as by: c. Giving quantitative measures of center (median and/or mean) and variability (interquartile range and/or mean absolute deviation), as well as describing any overall pattern and any striking deviations from the overall pattern with reference to the context in which the data were gathered.

Current Standard

6.SP.B.5c Summarize numerical data sets in relation to their context, such as by: c. Giving quantitative measures of center (median and/or mean) and variability (**range**), as well as describing any overall pattern and any striking deviations from the overall pattern with reference to the context in which the data were gathered.



Revisions to Math Standards

Specific to

9–12

- Revised scope and clarifications
- Revisions for Algebra II and Integrated III
- Restructured additional Mathematics courses to reflect college and career readiness

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Grades 9–12: Overarching Revisions

- Supporting and additional work of the grade is combined as supporting work of the grade
- Removed or shifted a small number of standards to the major work of the grade to streamline vertical progression
- Revised language and examples to provide clarity and continuity
- Shifted a small number of supporting work of the grade standards to the additional mathematics courses
- Restructured additional courses to reflect college and career readiness



Grades 9–12: Overarching Revisions

- Supporting and additional work of the grade is combined as supporting work of the grade
- Removed or shifted a small number of standards to the major work of the grade to streamline vertical progression
- Revised language and examples to provide clarity and continuity
- Shifted a small number of supporting work of the grade standards to the additional mathematics courses
- Restructured additional courses to reflect college and career readiness



Grades 9–12: Overarching Revisions

- Supporting and additional work of the grade is combined as supporting work of the grade
- Removed or shifted a small number of standards to the major work of the grade to streamline vertical progression
- Revised language and examples to provide clarity and continuity
- Shifted a small number of supporting work of the grade standards to the additional mathematics courses
- Restructured additional courses to reflect college and career readiness



Grades 9–12: Sample Revisions

Former Standard

G.SRT.8 Use trigonometric ratios and the Pythagorean Theorem to solve right triangles in applied problems.

Current Standard

G.SRT.C.8 *Know and* use trigonometric ratios and the Pythagorean Theorem to solve right triangles in applied problems.



Grades 9-12: Overarching Revisions

- Supporting and additional work of the grade is combined as supporting work of the grade
- Removed or shifted a small number of standards to the major work of the grade to streamline vertical progression
- Revised language and examples to provide clarity and continuity
- Shifted a small number of supporting work of the grade standards to the additional mathematics courses
- Restructured additional courses to reflect college and career readiness



Grades 9–12: Sample Revisions

Moved Standard

From:

A2.F.TF.5

M3.F.TF.5

To:

P.F.TF.A.4 Choose trigonometric functions to model periodic phenomena with specified amplitude, frequency, and midline.



Grades 9–12: Overarching Revisions

- Supporting and additional work of the grade is combined as supporting work of the grade
- Removed or shifted a small number of standards to the major work of the grade to streamline vertical progression
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- Shifted a small number of supporting work of the grade standards to the additional mathematics courses
- Restructured additional courses to reflect college and career readiness



Additional Mathematics Courses Rationale

- High expectations
- Retention of rigorous standards
- Clearly defined and coherent pathways
- Equity and opportunity
- Aligned with **student interest** in postsecondary fields
- Shift to a discipline- and career-based pathway



Additional Mathematics Courses

- Advanced Algebra and Trigonometry
- Discrete Math
- Finite Math
- Bridge Math
- Pre-Calculus
- Statistics
- Calculus



Additional Mathematics Courses

- Applied Mathematical Concepts (New Course)
- Bridge Math
- Pre-Calculus
- Statistics
- Calculus



Standards Comparison Activity

- Compare the 2016-17 standards to the revised standards for your assigned grade or course.
- Highlight any changes in the 2017-18 column.



Standards Comparison Activity

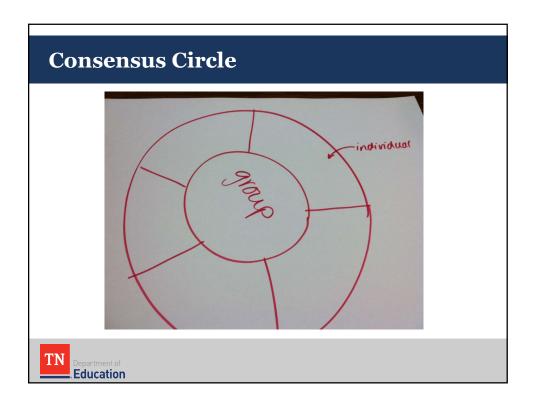
- If a standard is in the 2016-17 document, but not in the 2017-18 document, place a check in the "Dropped from Course" column.
- If a standard was not in the 2016-17 document, but is now in the 2017-18 document, place a check in the "Added to Course" column.
- If a standard was revised in any way (recoded, changes to the standard itself, moving examples from the standard to "Scope and Clarifications," etc.), place a check in the "Revised Or Refined" column.
- If a standard was not revised in any way, place a check in the "No Change" column.

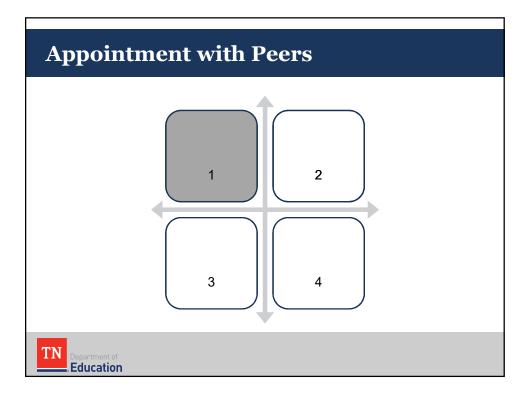


Standards Comparison Activity

- If you had to summarize the revisions to these selected standards in twenty words or less, what would you say?
- Write your response to the question in the participant manual.







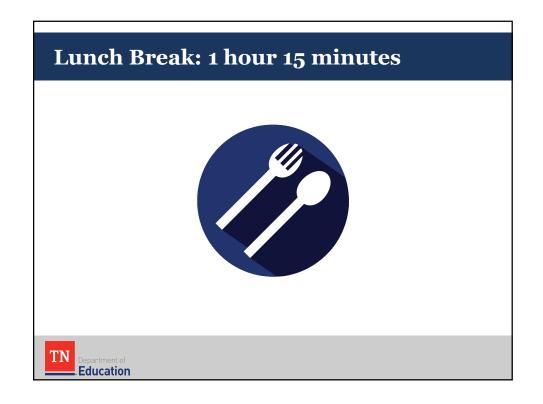
Module 3 Review

- The instructional shifts remain the same and are still the focus of the standards.
- The revised standards represent a stronger foundation that will support the progression of rigorous standards throughout the grade levels.
- The revised standards improve connections:
 - within a single grade level, and
 - between multiple grade levels.



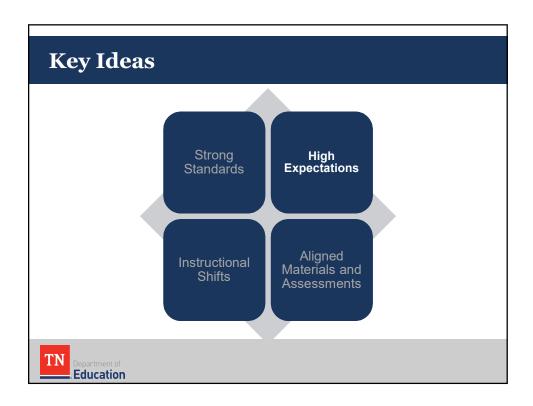
Part One Strong Standards Standards are the bricks that should be masterfully laid through quality instruction to ensure that all students reach the expectation of the standards.

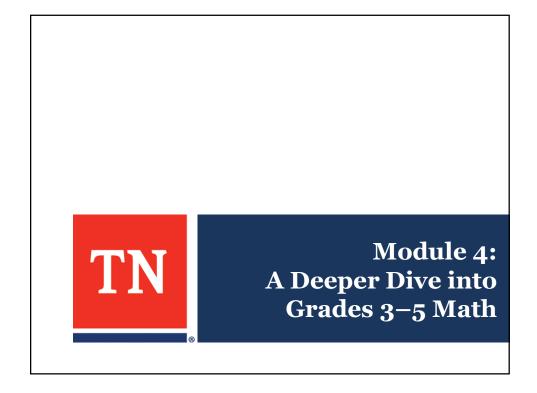
Education











Goals

- Concisely describe a course based on its introduction.
- Develop a means for deconstructing standards to determine the mathematical emphasis of the standard its intent and purpose.
- Use the KUD approach to guide planning, instruction, and assessment.





Seeing the Big Picture

Closer Look

Take a few minutes to read the Overview page for your grade level (the outline only) and think about how this relates to the overarching revisions we have just seen.

Grade 3 - p. 35 Grade 4 - p. 45 Grade 5 - p. 55



What Would You Tweet?

Summarize your course in 140 characters. Write a tweet that will inform others regarding what is included in your course.







Intent and Purpose

Intent and Purpose

"With my ears to the ground, listening to my students, my eyes are focused on the mathematical horizon."

- Ball (1993)



Analyzing Standards

5.NF.B.5 Interpret multiplication as scaling (resizing).

- a. Compare the size of a product to the size of one factor on the basis of the size of the other factor, without performing the indicated multiplication. For example, know if the product will be greater than, less than, or equal to the factors.
- b. Explain why multiplying a given number by a fraction greater than 1 results in a product greater than the given number (recognizing multiplication by whole numbers greater than 1 as a familiar case); explain why multiplying a given number by a fraction less than 1 results in a product less than the given number; and relate the principle of fraction equivalence $\frac{a}{b} = \frac{a \times n}{b \times n}$ to the effect of multiplying $\frac{a}{b}$ by 1.



Expectations of the Student

5.NF.B.5 Interpret multiplication as scaling (resizing).

- a. Compare the size of a product to the size of one factor on the basis of the size of the other factor, without performing the indicated multiplication. For example, know if the product will be greater than, less than, or equal to the factors.
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The Verbs Lead to the Nouns (or Noun Phrases)

- As noted, the verbs raise the questions of "what" leading one to next highlight the associated nouns.
- One may wish to highlight what might be termed a noun phrase instead of trying to be exact on the object of the verb. Remember that we are trying to understand the intent and purpose of the standard.
- There is also a temptation to almost highlight everything!
 Let's limit ourselves to the verbs and the nouns connected to them.



Highlighting Verbs: Expectations of the Student

5.NF.B.5 Interpret multiplication as scaling (resizing).

- a. Compare the size of a product to the size of one factor on the basis of the size of the other factor, without performing the indicated multiplication. For example, know if the product will be greater than, less than, or equal to the factors.
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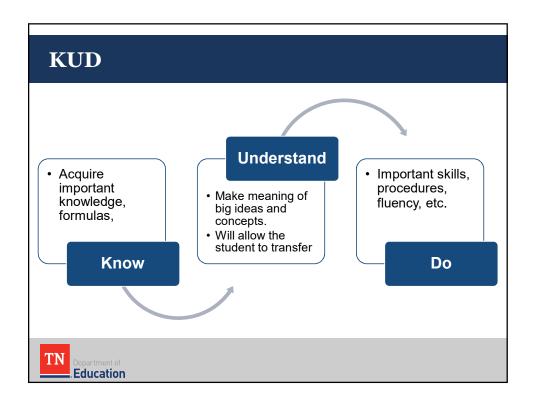


From Standard to Instruction: KUD

Know, Understand, and Do

- What is it that the standard wants the student to know, understand, and do?
- KUD helps to maintain focus in differentiated instruction
 - **Know**: facts, vocabulary, properties, procedures, etc.
 - Understand: concepts, ideas, etc.
 - **Do**: tasks, approaches, assessment problems, etc.
- The two go together: What is the intent and purpose of the standard and how do I put this into instructional form?





Summary of the Intent and Purpose of the Standard

- Write a brief description of each part of KUD with respect to this standard.
- What does the math look like? What vocabulary stands out? Any symbolism to be understood or other literacy skills needed?
- Can you now write an I Can statement and/or an Essential Question based on our understanding of the standard and the focus that KUD gives us?



What Do Students Understand?

- I can reason about the sizes of products based on the given factors.
- I can determine if the product will be greater than, less than, or equal to the factors.
- I can explain why the product of multiplying a fraction greater than 1 by a whole number is greater than the whole number.
- I can explain why the product of multiplying a fraction less than 1 by a whole number is less than the whole number.
- I can relate the principle of fraction equivalence to the effect of multiplying a fraction by 1.



What Do Students Understand?

- How might I determine the size of products based on the given factors?
- How might I determine if the product will be greater than, less than, or equal to the factors?
- Explain why the product of multiplying a fraction greater than 1 by a whole number is greater than the whole number?
- Explain why the product of multiplying a fraction less than 1 by a whole number is less than the whole number?
- How might I relate the principle of fraction equivalence to the effect of multiplying a fraction by 1?



Grade-Specific Examples

You try it!
You will be given a standard for your grade level.

3.NF.A.1

4.NF.B.4 (a only)

5.NF.B.4 (a only)



Analyzing Your Standard

- First, highlight verbs that speak to what the student will do.
- Second, highlight the nouns (noun phrases) connected to the verbs.
- Third, KUD, jot down what the students are to know, understand, and do (brief descriptions will do).
- Fourth, determine what the math will look like and touch on vocabulary and literacy skills needed.
- Now, write an I CAN statement and/or essential question that will be used in determining student mastery.



Gallery Walk

Please provide any comments or questions on Post-Its and put them on the chart paper.





Gallery Walk Debrief

- Small Group Discussion
 - Review the feedback you were given.
 - What are your key takeaways?

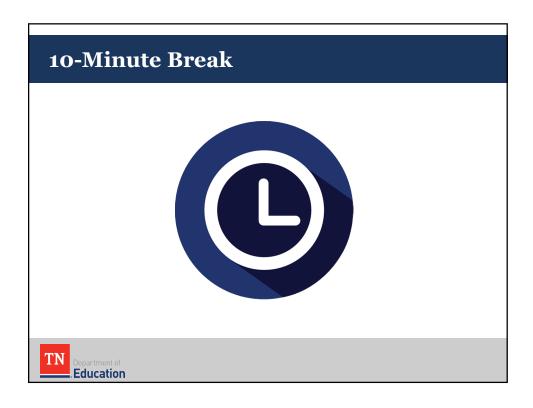


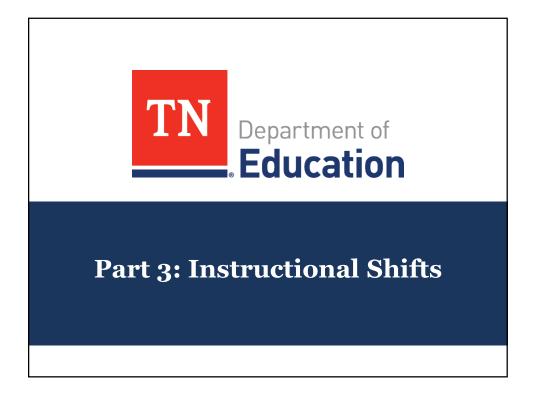
Module 4 Review

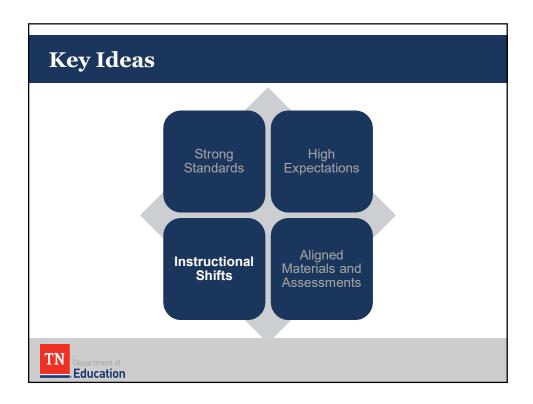
- Concisely describe a course based on it's introduction.
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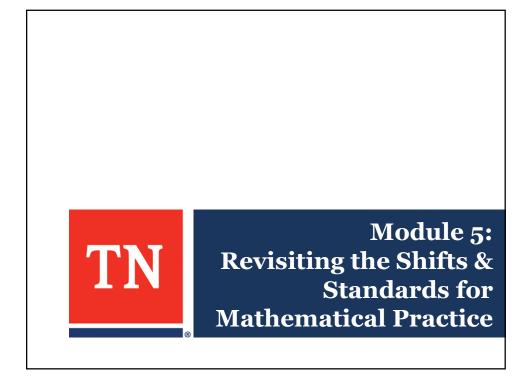












Goals

- Revisit the concepts of focus, coherence, and rigor and how they play out in instruction.
- Discuss the purpose and place of the content and practice standards.
- Focus on two areas of mindset: praise and mistakes.
- Share instructional strategies related to the Standards for Mathematical Practice.
- Discuss research on the influence of mindsets in the math classroom.



The Standards for Mathematical Practice

- Why do we have the standards?
- Tell us what students should know and be able to do
- So, what should students know and do?
 - Content Standards
 - Mathematics Practice Standards
 - Literacy Skills
- Knowing that these are WHAT students need to learn, teachers determine HOW to teach these.



Standards for Mathematical Practice

Standards for Mathematical Practice

- 1. Make sense of problems and persevere in solving them.
- 2. Reason abstractly and quantitatively.
- 3. Construct viable arguments and critique the reasoning of others.
- 4. Model with mathematics.
- 5. Use appropriate tools strategically.
- 6. Attend to precision.
- 7. Look for and make use of structure.
- 8. Look for and express regularity in repeated reasoning.



Mindset

- The TN Academic Standards for Mathematics may seem challenging for students whose mindset has been fixed by their past experiences in mathematics classrooms.
- As teachers, we are best positioned to influence students' mathematical mindsets through our actions/practices in the mathematics classroom.



Fixed Mindset vs. Growth Mindset

Fixed mindset

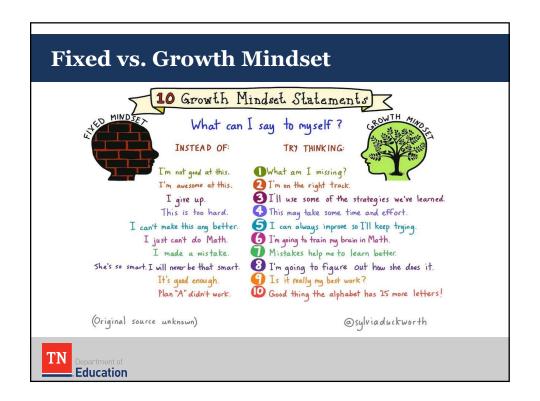
Intelligence is a fixed trait. You cannot change it.

Growth mindset

You can grow your intelligence through effort.



Study of Praise and Mindsets PRASE A STUDY BY CAROL DWECK TrainUgly.com

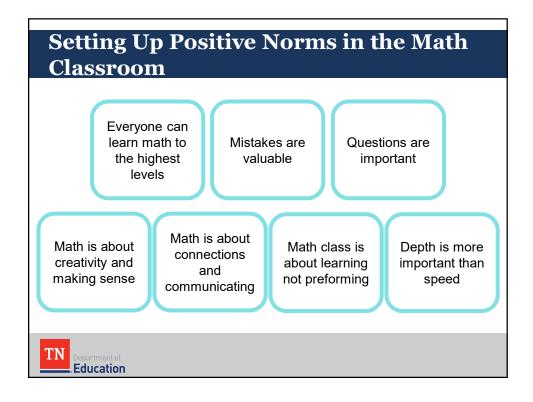


Why Address Mindsets?

"If there's a threat of being wrong every time I raise my hand, and being wrong is a bad thing, then very quickly I decide math isn't for me, I don't like this, I'm not a smart person".

—Noah Heller, Harvard Graduate School of Education





Instructional Shifts

Focus

 The standards are focused on fewer topics so that students can dig deeper within the mathematics.

Coherence

Topics within a grade are connected to support focus.
 Additionally, standards are linked across grades to ensure vertical coherence.

Rigor

 The standards set expectations for a balanced approach to pursuing conceptual understanding, procedural fluency, application, and modeling.



Expectation One: Focus

- In your grade level groups, discuss ways you could respond if someone asks you the following question, "Why focus? There's so much math that students could be learning. Why limit them?"
- Review Practicing with the Shifts in the participant manual and answer the question, 'Which 2 of the following represent areas of major focus for the indicated grade?'



Expectation One: Focus

| 3 | Multiply and divide within 100 | Students will work with central tendency in middle school, when they have developed solid computational skills and can use authentic data. | Develop understanding of fractions as numbers |
|---|---|--|--|
| 4 | Transformations are part of the major work of 8th grade. | Generalize place value understanding for multi-digit whole numbers | Extend understanding of fraction equivalence and ordering |
| 5 | Finding probability of an event occurs in 7th grade where it supports the major work of proportional reasoning. | Understand the place value system | Apply and extend previous understandings of multiplication and division to multiply and divide fractions |



Expectation Two: Coherence

• In the participant manual, copy all of the standards related to multiplication and division of fractions and note how coherence is evident in these standards. Note also standards that are outside of the Number and Operations—Fractions domain but are related to, or in support of, fractions.



Expectation Two: Coherence

| 3 | various | Standards that relate to the foundations of being able to multiply and divide fractions found in 3.OA and 3.NF | |
|---|--------------------|--|--|
| 4 | 4.NF.1 | Recognize & generate equivalent fractions | |
| 4 | 4.NF.4 a, b & c | Apply and extend previous understandings of multiplication to multiply a fraction by a whole number | |
| 4 | 4.MD.2 | Use 4 operations to solve word problems involving simple fractions | |
| 5 | 5.NF.3 | Interpreting a fraction as division of the numerator by the denominator. | |
| 5 | 5.NF.4 | Apply & extend previous understandings of multiplication to multiply a fraction or whole number by a fraction | |
| 5 | 5.NF.5 | Interpret multiplication as scaling (resizing) | |
| 5 | 5.NF.6 | Solve real word problems involving multiplication of fractions and mixed numbers | |
| 5 | 5.NF.7 | Apply and extend previous understandings of division to divide unit fractions by whole numbers and whole numbers by unit fractions | |
| | | | |



Expectation Three: Rigor

- Make a true statement: Rigor = ___+ __+ ___+
- In your groups, discuss ways to respond to one of the following comments: "These standards are expecting that we just teach rote memorization. Seems like a step backwards to me." Or "I'm not going to spend time on fluency—it should just be a natural outcome of conceptual understanding."
- The shift towards rigor is required by the Standards. Find and copy standards which specifically set expectations for each component of rigor.



Expectation Three: Rigor

Grade 3 standards that require **fluency**:

Grade 3: 3.OA.7; 3.NBT.2

Grade 3 standards that require **deep conceptual understanding**:

Grade 3: 3.OA.1-2, 5-6, 9; 3.NBT.1, 3.NF.1-3, 3.MD.5, 7; 3.G.1

Grade 3 standards that require application:

Grade 3: 3.OA.3,8; 3.MD.1-4,8



Turn & Talk

• What do these instructional shifts look like in the classroom?





Module 5 Review

- We connected the instructional shifts to the standards and our classroom practices.
- We've explored students' mathematical mindsets.
- We shared instructional strategies related to the Standards for Mathematical Practice





Module 6: Literacy Skills for Mathematical Proficiency

Goal

 Develop a better understanding of the Literacy Skills for Mathematical Proficiency.



Literacy in your Math Classroom

Reflect on ways literacy skills are already present in your mathematics classroom.





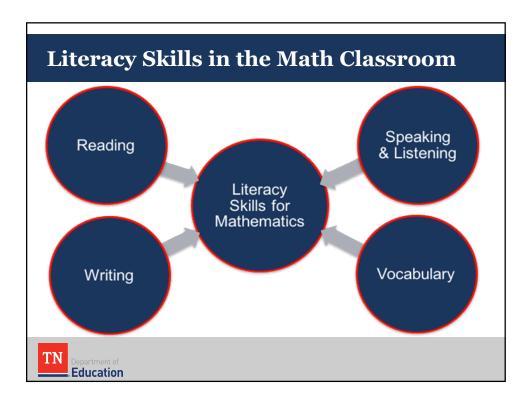
Literacy Skills for Math Proficiency

Communication in mathematics requires literacy skills in reading, vocabulary, speaking, listening, and writing.

Literacy Skills for Mathematical Proficiency

- 1. Use multiple reading strategies.
- 2. Understand and use correct mathematical vocabulary.
- 3. Discuss and articulate mathematical ideas.
- 4. Write mathematical arguments.

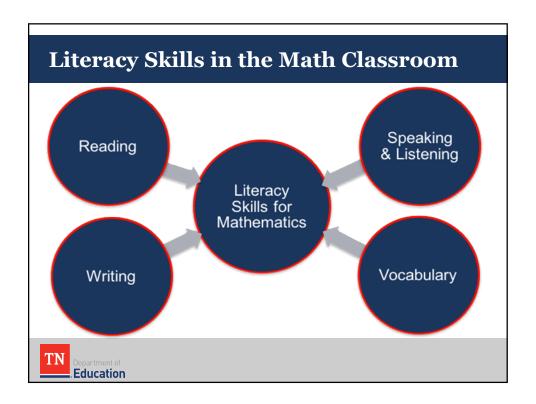




Group Activity

- Divide into groups.
- Each group will be assigned one literacy topic.
- Each group will read and annotate the paragraph on that topic in the Math Standards Document (pg. 13–14).
- Use chart paper to create a supporting document to share the ideas from your topic with the group.





Vocabulary

"Students must be taught that the language we read and speak in mathematics class is actually a technical jargon, even though it may look and sound like regular English."

-Hersh, 1997



Mathematics Vocabulary

- Student achievement is dependent upon students' reading comprehension and content area learning.
- Math vocabulary is decontextualized because they are not in everyday conversations.
- Mathematical terms can have specific meanings (i.e., average, reflection).
- Students need to develop a conceptual meaning in order to read and use the words accurately.



Four Stages of Word Knowledge

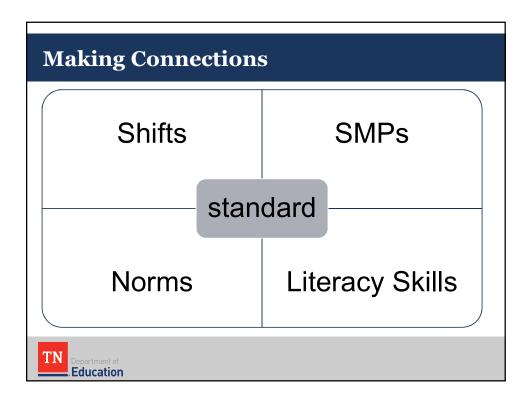
- 1. Students have never encountered the word before.
- 2. Students have seen/heard the word but do not know the definition.
- 3. Students know the word but rely on context to define it.
- 4. Students know the word and can use it comfortably.



Vocabulary

- Symbols are used as language.
- Many mathematical terms have different meanings in everyday use.
- Can you think of any examples?





Module 6 Review

- Literacy skills in the math classroom will support students' understanding of the content standards.
- When students can read, write, and speak about math ideas, connections are made between concepts.



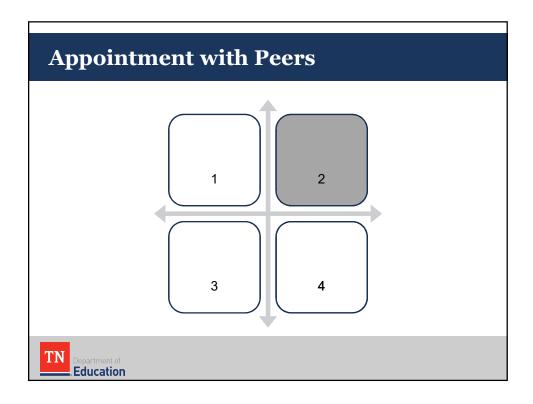
Part Three



Instructional Shifts

The instructional shifts are an essential component of the standards and provide guidance for how the standards should be taught and implemented.





What to Expect: Day 2

- Dig more deeply into assessments and question development.
- Explore what it means to assure alignment of curriculum to standards.
- Explore how to begin to develop instructional planning.







Districts and schools in Tennessee will exemplify excellence and equity such that all students are equipped with the knowledge and skills to successfully embark on their chosen path in life.

Excellence | Optimism | Judgment | Courage | Teamwork